Solvency capital estimation and risk measures

Antoni Ferri (RFA-IREA, XREAP)
Montserrat Guillén (RFA-IREA, XREAP)
Lluís Bermúdez (RFA-IREA, XREAP)
Solvency Capital estimation and Risk Measures
Antoni Ferri $^a,^1$, Montserrat Guillén $^a$, Lluís Bermúdez $^b$

$^a$ Departament d’Econometria, Estadística i Economia Espanyola. RISC-IREA. University of Barcelona. Spain
$^b$ Departament de Matemàtica Financera i Actuarial. RISC-IREA. University of Barcelona. Spain

This paper examines why a financial entity’s solvency capital estimation might be underestimated if the total amount required is obtained directly from a risk measurement. Using Monte Carlo simulation we show that, in some instances, a common risk measure such as Value-at-Risk is not subadditive when certain dependence structures are considered. Higher risk evaluations are obtained for independence between random variables than those obtained in the case of comonotonicity. The paper stresses, therefore, the relationship between dependence structures and capital estimation.

**Keywords:** Solvency II, Solvency Capital Requirement, Value-at-Risk, Tail Value-at-Risk, Monte Carlo, Copulas

1 Introduction

Recent years have seen the development of regulatory frameworks designed to guarantee the financial stability of banking and insurance entities around the world. Europe developed Basel II and, more recently, Basel III for its banking market, and parallel to these accords drew up the Solvency II directive in 2010 for its insurance market and the Swiss Solvency Test in Switzerland. The regulatory frameworks seek to establish what might be considered a reasonably amount of capital (referred to as Solvency Capital in Basel II and III and as Solvency Capital Requirement in Solvency II and the Swiss Solvency Test) to put aside to ensure financial stability in the case of adverse fluctuations on losses. This quantity must reflect the entity’s specific risk profile and, under the aforementioned frameworks, it can be arrived at by applying either the Standard Model proposed by the regulator or an Internal Model proposed by the entity itself. In the later case, a number of requirements must first be satisfied before the model can be used for the purposes of capital estimation. In the European frameworks is regulated by the calibration of a risk measurement given a confidence level over a given time horizon.

In this paper we focus our attention on the European insurance market, and more specifically in non-life underwriting risk, in relation to the Solvency II and Swiss Solvency Test regulations. Under both frameworks, the total capital estimation is obtained by aggregating individual capitals requirements arising from a company’s various sources of risk, based on the correlation between them as defined by the Standard Model.

As a means of aggregating risks, we proposed a simulation of a multivariate random variable where each marginal distribution function represents the claims of a

---

$^1$Corresponding Author. Departament d’Econometria, Estadística i Economia Espanyola, Universitat de Barcelona, Diagonal 690, 08034-Barcelona, Spain. Tel.:+34-93-4034853; fax: +34-93-4034892; e-mail: tonoferri@ub.edu. This research is sponsored by the Spanish Ministry of Science ECO2010-21787
given line of business. We simulate a sample of this multivariate random variable taking into account the correlation between lines of business and, then, we aggregate the results of each simulated claim by line of business in order to obtain the distribution of the total claims. Finally, we estimate the capital requirements by applying a risk measure over the total claims distribution.

By representing an example of a multivariate random variable simulation we show that under certain assumptions there are risk measures that fail to satisfy the subadditive property. This is typically the case where there is a very heavy tailed or skewed distribution on the margin and/or in which a special dependence structure is assumed for its joint distribution. Such circumstances can lead to an underestimation of the solvency capital if we incorrectly assimilate a risk measurement to the capital requirements, i.e., the appropriate distribution is not fitted to the marginals or the joint behavior of the marginal distributions is unknown.

The paper also emphasizes typical misunderstanding in the meaning of risk measures and the relationship between these risk measures and the underlying dependence structures of the variables, which represents the sources of risk.

2 Misunderstanding in the meaning of Value-at-Risk measure

Risk measures are typically employed to determine the amount of capital that should be aside to cover unexpected losses. Artzner et al. (1999) proposed a number of desirable properties that a risk measure should satisfy in order to be considered a coherent risk measure. One such property, that of subadditivity, captures the idea of diversification across random variables since in the words of Artzner et al. (1999): "...the merger [of two risks] does not create extra risk". Suppose we have $n$ random variables, $X_i, i = 1,...,n$ and its sum, $S = \sum_{i=1}^{n} X_i$; then we say that risk measure $\rho$ has the subadditivity property if and only if for all $X_i$

$$\rho(S) \leq \sum_{i=1}^{n} \rho(X_i).$$

(1)

Although several risk measures are available, here we focus on two that are on loss distribution, namely Value-at-Risk and Tail Value-at-Risk. These risk measures seek to describe how risky a portfolio is. Of the two, the most frequently adopted is the Value-at-Risk measure given that it is employed under Basel III and Solvency II as a tool for calibrating the solvency capital requirements. Value-at-Risk and its properties have been widely discussed (see Jorion, 2007). The Value-at-Risk measure is simply a quantile of a distribution function. However, it is not a coherent risk measure since it does not satisfy condition (1) for all $X_i$, although it does in the case in which $X_i$ are normally distributed and, more generally, in the case in which elliptical distributions are considered for $X_i$ as is shown in Fang et al. (1990) and Embrechts et al. (2002). Formally, given a confidence level $\alpha \in [0,1]$, Value-at-Risk is defined as the infimum value of the distribution of a random variable $X$ such that the probability that a value $x$ exceeds a certain threshold
$x$ is no greater than $1 - \alpha$. Usually this probability is taken to be 0.05 or less.

$$VaR^\alpha(X) = \inf \{x/P(X > x) = 1 - \alpha\} = F_X^\alpha(\alpha)$$

(2)

where $F_X(x)$ denotes the distribution function of $X$ and $F_X^\alpha(\alpha)$ denotes the inverse distribution function of $F_X(x)$.

It is common to choose $1 - \alpha$ based on a very large period. For example, under the Solvency II directive, this choice is made on the basis of an occurrence of an event every two hundred years, i.e., a probability of 0.5%. For this reason, this risk measure is known as a frequency measure. It describes the distribution up to the $\alpha$-th percentile, but it provides no information as to how the distribution behaves at higher percentiles.

Unlike the Value-at-Risk measure, the Tail Value-at-Risk describes the behavior of the tail of the distribution. This risk measure is defined, therefore, as the expected value of all percentiles higher than the Value-at-Risk. Formally,

$$TVaR^\alpha(X) = E[X|X \geq VaR^\alpha(X)]$$

(3)

where $E[\cdot | \cdot]$ denotes the conditional expectation operator.

Thus, while two different distributions might have the same Value-at-Risk for a given a confidence level, their Tail Value-at-Risk may differ due to a different heaviness of the tail of the distribution. The fact of having to consider not just the choice of $1 - \alpha$ but also the values of the distribution higher than the $\alpha$-th percentile means the Tail Value-at-Risk is known as a severity risk measure. Likewise, the Tail Value-at-Risk measure is a subadditive and coherent since it satisfies property (1), as is shown in Embrechts et al. (2005).

Despite the mathematical principles underpinning the Value-at-Risk and Tail Value-at-Risk measures, a misunderstanding arises when seeking to apply them (specially, in the case of the former) to capital requirements. It is common to interpret Value-at-Risk as the value that will not be exceeded with a probability $\alpha$. If, as is usual, the random variable is considered as the loss of a portfolio, this definition is equivalent to the loss that will not be exceeded with a probability of $\alpha$, or the maximum loss given $\alpha$ as pointed out by Jorion (2007). Yet, this interpretation is not strictly correct since maximum loss is not generally given by Value-at-Risk for a given confidence level as we shall see below.

Inequality (1) shows an upper bound for $\rho(S)$ which is $\sum_{i=1}^{n} \rho(X_i)$. A typical misunderstanding arises from this bound given that only in cases of diversifiable risks can such a bound occur. In instances of non-diversifiable risks this bound fails. As Embrechts et al. (2003) showed, if we consider Value-at-Risk as a risk measure and a sequence of comonotonic random variables $X_i, i = 1, ..., n$ then $VaR(S) = VaR(\sum_{i=1}^{n} X_i) = \sum_{i=1}^{n} VaR(X_i)$, which is known as the comonotonic bound. But this is not the worst possible case since comonotonicity does not necessarily result in the worst loss a company might suffer. Dependence structures between random variables $X_i$ might be found so that the Value-at-Risk of the sum of them exceeds the comonotonic bound. Translating this to the definition of Value-at-Risk we can conclude that it is possible to have greater losses than those arising from the comonotonic case given $\alpha$. Then
\[ \sum_{i=1}^{n} VaR(X_i) \] is not the maximum loss we could have given \( \alpha \).

Generally, Value-at-Risk fails to be a sub-additive risk measure in those cases where we have very heavy-tailed random variables, which is the case of those variables representing catastrophic or operational risks. It also fails in the case of skewed random variables and in some instances in which special dependence structures are imposed on the joint behavior of margins. Embrechts et al. (2005) showed that when Pareto random variables are considered, Value-at-Risk fails to be subadditive. Moreover, when the infinite mean case is considered, i.e., a tail-parameter of Pareto distribution is equal to one for all random variables considered, Value-at-Risk fails to be sub-additive at all confidence levels, otherwise, there’s a confidence level up to which Value-at-Risk is sub-additive and beyond which it is not.

In short, the estimation of capital requirements using a risk measure should be approached with caution since the resulting valuation might underestimate the capital needs depending on the joint distribution of the random variables representing the implicit risks within a company as well as on its individual statistical distributions. Therefore, risk measurements derived from non coherent risk measures could lead the company to financial and solvency instability.

### 3 A non-subadditivity example for Value-at-Risk

In this section we present an example in which we demonstrate that while the Value-at-Risk measure fails to be subadditive, the Tail Value-at-Risk measure satisfies the property of subadditivity. We use a historical non-life insurance market data set for Spain corresponding to the period 2000 to 2010. The data were obtained from public information published at the website of the Dirección General de Seguros (DGS)\(^2\). The data represents the yearly annual aggregate claims and three lines of business are considered (see Table 1 for their descriptive statistics\(^3\)). A complete description of the risks included in each line of business can be found in the QIS-5 Technical Specifications, CEIOPS (2010).

| Table 1: Descriptive statistics \(*\) of the yearly annual aggregate \(**\) claims by line of business |
|---------------------------------|----------|----------|----------|----------|----------|----------|----------|
| Motor, third party liability    | Min.     | 1st Qu.  | Median   | Mean     | Sd       | 3rd Qu.  | Max.     |
| Fire and other property damage | 4.286     | 4.904    | 5.182    | 5.085    | 0.332    | 5.318    | 5.439    |
| Third party liability          | 2.337     | 3.006    | 3.740    | 3.539    | 0.723    | 4.067    | 4.544    |
|                                 | 0.552     | 0.684    | 0.819    | 0.842    | 0.195    | 1.011    | 1.084    |

Source: Own source from DGS / \(*\) thousand millions euros / \(**\) deflated

We assume that each line of business behaves statistically as a generalized Pareto random variable. The parameters resulting from fitting the data to the Pareto distribution are shown in Table 2.

---

\(^2\) www.dgsfp.meh.es

\(^3\) Minimum (Min.), Quartile (Qu.), Standard deviation (Sd), Maximum (Max.)
Table 2: Generalized Pareto shape and scale * parameters

<table>
<thead>
<tr>
<th></th>
<th>Shape</th>
<th>Scale</th>
</tr>
</thead>
<tbody>
<tr>
<td>Motor, third party liability</td>
<td>0.93</td>
<td>0.30</td>
</tr>
<tr>
<td>Fire and other property damage</td>
<td>0.95</td>
<td>0.23</td>
</tr>
<tr>
<td>Third party liability</td>
<td>0.75</td>
<td>0.19</td>
</tr>
</tbody>
</table>

*thousand millions euros

After fitting the data of each line of business to its corresponding distribution, we performed a multivariate Monte Carlo simulation and we compute the Value-at-Risk and the Tail Value-at-Risk for several confidence levels. For the joint behavior of risks we imposed several copulas, which in fact entails considering several different dependence structures. An introduction to multivariate models and dependence concepts and their properties can be found in Nelsen (2006) and Joe (1997). First, we established two extreme cases of dependence: comonotonicity and independence. We used the upper Fréchet copula, which reflects the case of comonotonicity between margins, and then we used the independence copula, which reflects the case of independence between margins. Finally, we employed two further copulas, the Clayton copula, a very right-skewed distribution, and the Frank copula, a symmetric but very heavy tailed distribution, with two dependence parameters (θ) each one.

Table 3 shows the results of Value-at-Risk and Tail Value-at-Risk for several confidence levels. Under the comonotonic assumption, which leads to the comonotonic bound, Value-at-Risk underestimates the risk (i.e., fails to be subadditive) compared to the independence, the Clayton and Frank copula cases at all confidence level up to some point between 0.90 and 0.99, and beyond which it Value-at-Risk satisfy the subadditivitiy property. The values in bold indicate where the subadditivity property fails to be satisfied compared with the case of comonotonicity.

Table 3: VaR and TVaR * from a simulation ** of a tridimensional multivariate distribution for several dependence structures and Pareto margins

<table>
<thead>
<tr>
<th>c.l.</th>
<th>independence copula</th>
<th>Clayton copula</th>
<th>Frank copula</th>
<th>comonotonic copula</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>θ = 1</td>
<td>θ = 2</td>
<td>θ = 1</td>
<td>θ = 2</td>
</tr>
<tr>
<td>0.8</td>
<td>3.41</td>
<td>3.53</td>
<td>3.57</td>
<td>3.45</td>
</tr>
<tr>
<td>0.9</td>
<td>6.36</td>
<td>6.78</td>
<td>6.99</td>
<td>6.59</td>
</tr>
<tr>
<td>0.99</td>
<td>47.69</td>
<td>49.6</td>
<td>50.7</td>
<td>50.02</td>
</tr>
<tr>
<td>0.999</td>
<td>396.05</td>
<td>396.45</td>
<td>421.82</td>
<td>371.26</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>c.l.</th>
<th>independence copula</th>
<th>Clayton copula</th>
<th>Frank copula</th>
<th>comonotonic copula</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>θ = 1</td>
<td>θ = 2</td>
<td>θ = 1</td>
<td>θ = 2</td>
</tr>
<tr>
<td>0.8</td>
<td>23.14</td>
<td>25.09</td>
<td>26.76</td>
<td>24.78</td>
</tr>
<tr>
<td>0.9</td>
<td>41.7</td>
<td>45.34</td>
<td>48.57</td>
<td>44.84</td>
</tr>
<tr>
<td>0.99</td>
<td>289.28</td>
<td>318.72</td>
<td>347.22</td>
<td>315.22</td>
</tr>
<tr>
<td>0.999</td>
<td>1868.51</td>
<td>2151.37</td>
<td>2419.51</td>
<td>2163.13</td>
</tr>
</tbody>
</table>

Source: Own source / *thousand millions euros / c.l.: confidence level / **100,000 simulations
Since, Tail Value-at-Risk is a subadditive measure of risk, all values under independence case, as well as those for the Clayton and Frank copula assumptions are, as expected, lower than those in the comonotonic case at all confidence level. In the Tail Value-at-Risk case, the more dependence assumption implies higher values of risk measurements at all confidence levels.

4 Implications for Risk Management

New regulatory frameworks in Europe establish the capital requirements that financial companies need to maintain in order to ensure acceptable levels of solvency. These requirements are calibrated by applying a risk measure based on the distribution of a random variable that represents the total losses a company would suffer.

Typically, in the field of risk management, managers are aware of the individual risks for which they have responsibility, but are unaware of the relationship between the sources of risk that they manage and those arising from other departments or other areas within the same company. This means that the joint behavior of the random variables representing the different sources of risk remains unknown. As such, the process of aggregating risk measurements to obtain an global capital requirement is complex and difficult to address.

As consequence of this, it's usual for risk managers to obtain the risks measurements of each variable that represent a single source of risk considered and after that add them up to obtain a single amount and assimilate it to the regulatory capital.

In so doing, if companies choose a non coherent risk measure (as defined by Artzner et al., 1999) such as Value-at-Risk, (thereby adhering to Solvency II or Basel III criteria), they may overlook a number of crucial points. First, they may overlook the tail behavior of each random variable considered individually, which means, they fail to incorporate the possibility of severe losses that could greatly undermine the company's solvency. Second, by summing up risk measurements, such as those resulting from the Value-at-Risk, a company implicitly assumes, perhaps inadvertently, that its random variables are comonotonic, which is in conflict with the idea of ignoring the joint behavior of variables. Even in those instance in which risk managers believe that the joint behavior is comonotonic, it is possible to suffer worse losses than those that are consequence of summing the Value at Risk measurements derived from comonotonic random variables, as shown in the example in the previous section (see Table 3). In this example, even when the random variables are independent, the Value at Risk of the sum of random variables is greater than it is in the case of comonotonicity at certain confidence levels.

This finding highlights not only the importance of choosing a coherent risk measure, but also the need, first, to select the right fit and distribution function so as to reflect correctly the joint behavior of sources of risk and their dependence structures; and, second, to select the right fit and distribution functions so as to reflect the margin behavior of each random variable representing a single sources of risk.

In example presented in Table 3, we used Pareto distributions for margins. When considering this distribution, it is possible to find cases in which we might have infinite
expected values or variance, which are extreme cases that cause non-subadditivity for the Value-at-Risk measure, but they are not the only cases in which this might occur. There are many risks, generally catastrophic risks, for which the Pareto distribution fits well, and for which the non-subadditivity property could fail when using non-coherent risk measures. Examples of the Pareto distribution being fitted to operational and catastrophic risks can be found in Guillén et al. (2011) and Sarabia et al. (2009), respectively.

A number of lessons can be drawn by those involved in risk management from the preceding analysis. First, knowledge of the joint statistic behavior of risks is essential when considering a company’s overall level of risk. This does not simply mean the need to estimate the correlation coefficients but also to consider underlying dependence structures. Second, although using a coherent risk measure such as the Tail Value-at-Risk leads to higher capital estimations than in the case when using the Value-at-Risk measure, it serves to ensure that capital requirements are not underestimated due to the property of subadditivity should the hypothesis regarding the joint behavior of sources of risk prove to be incorrect. However, errors in the model estimation could well lead to the real capital needs being underestimated, even though a coherent risk measure such as Tail Value-at-Risk has been used. Third, comonotonicity does not represent the worst possible scenario when estimating capital requirements using loss and risk measurements. This might appear counterintuitive, but managers of risks need to bear in mind that risks may well be superadditive as opposed to subadditive, and as such, no diversification effect occurs when several random variables are merged. Fourth, while it may appear obvious, differences in capital estimation derived from the application of different risk measures do not mean the portfolio has varying degrees of risk; rather what we see is simply different ways of measuring what might happen beyond a given threshold, i.e. the losses that would exceed the threshold in the case of the Value-at-Risk measure, and the severity of these losses beyond the threshold in the case of Tail Value-at-Risk measure.

Appendix

A multivariate simulation of the random variable was conducted using the R-Project software, version 2.13.1 and the copula package implemented therein. Below we describe the simulation performance.

A random variable $X$ has a Generalized Pareto distribution (GPD) if its distribution function is

$$G_{X, \xi, \beta}(x) = \begin{cases} 1 - \left(1 + \frac{\xi \cdot x}{\beta}\right)^{-\frac{1}{\xi}} & \text{if } \xi \neq 0 \\ 1 - \exp \left(-\frac{x}{\beta}\right) & \text{if } \xi = 0 \end{cases}$$

where $\xi$ the shape parameter and $\beta > 0$ the scale parameter.
The expected value $E[X]$ is

$$E[X] = \frac{\beta}{1 - \xi}$$

and the standard deviation is the scale parameter $\beta$.

The shape parameter can be estimated using maximum likelihood estimation or the method of moments. Using the moments estimation procedure, the shape parameter results in

$$E[X] = \frac{\beta}{1 - \xi} \Rightarrow \xi = \frac{-\beta}{E[X]} + 1 = -CoVa[X] + 1;$$

being $CoVa[X]$ the coefficient of variation of $X$.

Having estimated the sample expected value and the standard deviation for each line of business considered we obtain the coefficient of variation and construct a 2x3 matrix containing the coefficients of variation and standard deviation in each of the rows. The columns represent each one of the three line of business.

```
data<-read.table('CoV.csv', header=TRUE, sep=";")
data<-as.matrix(data)
```

The estimation of the shape and scale parameters becomes

```
shape1<-data[1,1]+1 # the shape parameter for the first margin.
shape2<-data[1,2]+1 # the shape parameter for the second margin.
shape3<-data[1,3]+1 # the shape parameter for the third margin.
scale1<-data[2,1] # the scale parameter for the first margin.
scale2<-data[2,2] # the scale parameter for the second margin.
scale3<-data[2,3] # the scale parameter for the third margin.
```

The comonotonic bound are derived from the sum of the $\alpha$-th quantiles of each marginal distribution. We compute the quantiles for each margin after simulating one thousand observations of the GPD for each margin given its corresponding parameters.

```
n=100000 # number of simulations.
l<-c(0.80,0.90,0.99,0.999) # vector of given confidence level.
pareto1<-rGPD(n,shape1, beta=scale1) # simulation for the first margin.
pareto2<-rGPD(n,shape2, beta=scale2) # simulation for the second margin.
pareto3<-rGPD(n,shape3, beta=scale3) # simulation for the third margin.
VaR1<-quantile(pareto1,l) # vector of Value-at-Risk for the first margin.
VaR2<-quantile(pareto2,l) # vector of Value-at-Risk for the second margin.
```
VaR3<-quantile(pareto3,l) # vector of Value-at-Risk for the third margin.

VaR_com<-VaR1+VaR2+VaR3# comonotonic bound vector.

When considering independence between the random variables, we obtain the Value-at-Risk and the Tail Value-at-Risk by simulating the three-dimensional Gaussian copula with Pareto margins given shape and scale parameters and dependence parameters (linear correlations) for the copula equal to zero.

corr<-c(0,0,0) # vector of linear correlations for the Gaussian copula.

copulagainaussian<-mvdc(normalCopula(corr,dim=3,dispstr ="un"),c(rep("GPD",3)),list(param1,param2,param3))

gaussian.sample<-rmvdc(copulagainaussian,1000000) # simulation of the copula.

VaR_ind<-quantile(gaussian.sample.aggrega,l)

TVaR_ind<-rep(0,4)
for(i in 1:4){ES<-mean(gaussian.sample.aggrega[gaussian.sample.aggrega>VaR_ind[i]])
TVaR_ind[i]<-ES}

VaR_ind # Value-at-Risk vector under independence assumption.

TVaR_ind # Tail Value-at-Risk vector under independence assumption.

The Tail Value-at-Risk under the comonotonicity assumption between random variables is obtained by simply setting a new correlation vector for the Gaussian copula, i.e, corr<-c(0.99999,0.99999,0.99999) as the comonotonic copula can be obtained when the dependence parameters of the Gaussian copula tend to one.

The Value-at-Risk and Tail Value-at-Risk for the Clayton and Frank copulas are obtained in a similar way but changing the kind of copula used and the corresponding dependence parameter. We show the Clayton copula case for a dependence parameter $\theta = 1$.

theta=1 # dependence parameter for the Clayton copula.
Copulaclayton<-mvdc(claytonCopula(theta,dim=3),c(rep("GPD",3)),
list(param1,param2,param3))
clayton.sample<-rmvdc(copulaclayton,1000000)
clayton.sample.aggrega<-rowSums(clayton.sample)
VaR_cl<-quantile(clayton.sample.aggrega,l)
TVaR_cl<-rep(0,4)
for(i in 1:4){
ES<-mean(clayton.sample.aggrega[clayton.sample.aggrega>VaR_cl[i]])}
TVaR_cl[i]<-ES

VaR_cl # Value-at-Risk vector under Clayton copula assumption.
TVaR_cl # Tail Value-at-Risk vector under Clayton copula assumption.

References

CREAP2006-01
Matas, A. (GEAP); Raymond, J.LL (GEAP)
"Economic development and changes in car ownership patterns"
(Juny 2006)

CREAP2006-02
Trillas, F. (IEB); Montolio, D. (IEB); Duch, N. (IEB)
"Productive efficiency and regulatory reform: The case of Vehicle Inspection Services"
(Setembre 2006)

CREAP2006-03
Bel, G. (PPRE-IREA); Fageda, X. (PPRE-IREA)
"Factors explaining local privatization: A meta-regression analysis"
(Octubre 2006)

CREAP2006-04
Fernández-Villadangos, L. (PPRE-IREA)
"Are two-part tariffs efficient when consumers plan ahead?: An empirical study"
(Octubre 2006)

CREAP2006-05
Artís, M. (AQR-IREA); Ramos, R. (AQR-IREA); Suriñach, J. (AQR-IREA)
"Job losses, outsourcing and relocation: Empirical evidence using microdata"
(Octubre 2006)

CREAP2006-06
Alcañiz, M. (RISC-IREA); Costa, A.; Guillén, M. (RISC-IREA); Luna, C.; Rovira, C.
"Calculation of the variance in surveys of the economic climate"
(Novembre 2006)

CREAP2006-07
Albalate, D. (PPRE-IREA)
"Lowering blood alcohol content levels to save lives: The European Experience”
(Desembre 2006)

CREAP2006-08
Garrido, A. (IEB); Arqué, P. (IEB)
“The choice of banking firm: Are the interest rate a significant criteria?”
(Desembre 2006)
CREAP2006-09
Segarra, A. (GRIT); Teruel-Carrizosa, M. (GRIT)
"Productivity growth and competition in spanish manufacturing firms: What has happened in recent years?"
(Desembre 2006)

CREAP2006-10
Andonova, V.; Díaz-Serrano, Luis. (CREB)
“Political institutions and the development of telecommunications”
(Desembre 2006)

CREAP2006-11
Raymond, J.L. (GEAP); Roig, J.L. (GEAP)
"Capital humano: un análisis comparativo Catalunya-España”
(Desembre 2006)

CREAP2006-12
Rodríguez, M. (CREB); Stoyanova, A. (CREB)
"Changes in the demand for private medical insurance following a shift in tax incentives”
(Desembre 2006)

CREAP2006-13
Royuela, V. (AQR-IREA); Lambiri, D.; Biagi, B.
"Economia urbana y calidad de vida. Una revisión del estado del conocimiento en España”
(Desembre 2006)

CREAP2006-14
Camarero, M.; Carrion-i-Silvestre, J.L. (AQR-IREA); Tamarit, C.
"New evidence of the real interest rate parity for OECD countries using panel unit root tests with breaks”
(Desembre 2006)

CREAP2006-15
Karanassou, M.; Sala, H. (GEAP); Snower, D. J.
"The macroeconomics of the labor market: Three fundamental views”
(Desembre 2006)
XREAP2007-01
Castany, L (AQR-IREA); López-Bazo, E. (AQR-IREA); Moreno, R. (AQR-IREA)
"Decomposing differences in total factor productivity across firm size"
(Març 2007)

XREAP2007-02
Raymond, J. Ll. (GEAP); Roig, J. Ll. (GEAP)
"Una propuesta de evaluación de las externalidades de capital humano en la empresa"
(Abril 2007)

XREAP2007-03
Durán, J. M. (IEB); Esteller, A. (IEB)
“An empirical analysis of wealth taxation: Equity vs. Tax compliance”
(Juny 2007)

XREAP2007-04
Matas, A. (GEAP); Raymond, J.Ll. (GEAP)
“Cross-section data, disequilibrium situations and estimated coefficients: evidence from car ownership demand”
(Juny 2007)

XREAP2007-05
Jofre-Montseny, J. (IEB); Solé-Ollé, A. (IEB)
“Tax differentials and agglomeration economies in intraregional firm location”
(Juny 2007)

XREAP2007-06
Álvarez-Albelo, C. (CREB); Hernández-Martín, R.
“Explaining high economic growth in small tourism countries with a dynamic general equilibrium model”
(Juliol 2007)

XREAP2007-07
Duch, N. (IEB); Montolio, D. (IEB); Mediavilla, M.
“Evaluating the impact of public subsidies on a firm’s performance: a quasi-experimental approach”
(Juliol 2007)

XREAP2007-08
Segarra-Blasco, A. (GRIT)
“Innovation sources and productivity: a quantile regression analysis”
(Octubre 2007)
SÈRIE DE DOCUMENTS DE TREBALL DE LA XREAP

XREAP2007-09
Albalate, D. (PPRE-IREA)
“Shifting death to their Alternatives: The case of Toll Motorways”
(Octubre 2007)

XREAP2007-10
Segarra-Blasco, A. (GRIT); Garcia-Quevedo, J. (IEB); Teruel-Carrizosa, M. (GRIT)
“Barriers to innovation and public policy in catalonia”
(Novembre 2007)

XREAP2007-11
Bel, G. (PPRE-IREA); Foote, J.
“Comparison of recent toll road concession transactions in the United States and France”
(Novembre 2007)

XREAP2007-12
Segarra-Blasco, A. (GRIT);
“Innovation, R&D spillovers and productivity: the role of knowledge-intensive services”
(Novembre 2007)

XREAP2007-13
Bermúdez Morata, Ll. (RFA-IREA); Guillén Estany, M. (RFA-IREA), Solé Auró, A. (RFA-IREA)
“Impacto de la inmigración sobre la esperanza de vida en salud y en discapacidad de la población española”
(Novembre 2007)

XREAP2007-14
Calaeys, P. (AQR-IREA); Ramos, R. (AQR-IREA), Suriñach, J. (AQR-IREA)
“Fiscal sustainability across government tiers”
(Desembre 2007)

XREAP2007-15
Sánchez Hugalbe, A. (IEB)
“Influencia de la inmigración en la elección escolar”
(Desembre 2007)
XREAP2008-01
Durán Weitkamp, C. (GRIT); Martín Bofarull, M. (GRIT) ; Pablo Martí, F.
“Economic effects of road accessibility in the Pyrenees: User perspective”
(Gener 2008)

XREAP2008-02
Díaz-Serrano, L.; Stoyanova, A. P. (CREB)
“The Causal Relationship between Individual’s Choice Behavior and Self-Reported Satisfaction: the Case of Residential Mobility in the EU”
(Març 2008)

XREAP2008-03
Matas, A. (GEAP); Raymond, J. L. (GEAP); Roig, J. L. (GEAP)
“Car ownership and access to jobs in Spain”
(Abril 2008)

XREAP2008-04
Bel, G. (PPRE-IREA) ; Fageda, X. (PPRE-IREA)
“Privatization and competition in the delivery of local services: An empirical examination of the dual market hypothesis”
(Abril 2008)

XREAP2008-05
Matas, A. (GEAP); Raymond, J. L. (GEAP); Roig, J. L. (GEAP)
“Job accessibility and employment probability”
(Maig 2008)

XREAP2008-06
Basher, S. A.; Carrión, J. Ll. (AQR-IREA)
Deconstructing Shocks and Persistence in OECD Real Exchange Rates
(Juny 2008)

XREAP2008-07
Sanromá, E. (IEB); Ramos, R. (AQR-IREA); Simón, H.
Portabilidad del capital humano y asimilación de los inmigrantes. Evidencia para España
(Juliol 2008)

XREAP2008-08
Basher, S. A.; Carrión, J. Ll. (AQR-IREA)
Price level convergence, purchasing power parity and multiple structural breaks: An application to US cities
(Juliol 2008)

XREAP2008-09
Bermúdez, Ll. (RFA-IREA)
A priori ratemaking using bivariate poisson regression models
(Juliol 2008)
XREP2008-10
Solé-Ollé, A. (IEB), Hortas Rico, M. (IEB)
Does urban sprawl increase the costs of providing local public services? Evidence from Spanish municipalities
(Novembre 2008)

XREP2008-11
Teruel-Carrizosa, M. (GRIT), Segarra-Blasco, A. (GRIT)
Immigration and Firm Growth: Evidence from Spanish cities
(Novembre 2008)

XREP2008-12
Duch-Brown, N. (IEB), García-Quevedo, J. (IEB), Montolio, D. (IEB)
Assessing the assignation of public subsidies: Do the experts choose the most efficient R&D projects?
(Novembre 2008)

XREP2008-13
Bilotkach, V., Fageda, X. (PPRE-IREA), Flores-Fillol, R.
Scheduled service versus personal transportation: the role of distance
(Desembre 2008)

XREP2008-14
Albalate, D. (PPRE-IREA), Gel, G. (PPRE-IREA)
Tourism and urban transport: Holding demand pressure under supply constraints
(Desembre 2008)
XREAP2009-01
Calonge, S. (CREB); Tejada, O.
“A theoretical and practical study on linear reforms of dual taxes”
(Febrer 2009)

XREAP2009-02
Albalate, D. (PPRE-IREA); Fernández-Villadangos, L. (PPRE-IREA)
“Exploring Determinants of Urban Motorcycle Accident Severity: The Case of Barcelona”
(Març 2009)

XREAP2009-03
Borrell, J. R. (PPRE-IREA); Fernández-Villadangos, L. (PPRE-IREA)
“Assessing excess profits from different entry regulations”
(Abril 2009)

XREAP2009-04
Sanromá, E. (IEB); Ramos, R. (AQR-IREA), Simon, H.
“Los salarios de los inmigrantes en el mercado de trabajo español. ¿Importa el origen del capital humano?”
(Abril 2009)

XREAP2009-05
Jiménez, J. L.; Perdiguero, J. (PPRE-IREA)
“(No)competition in the Spanish retailing gasoline market: a variance filter approach”
(Maig 2009)

XREAP2009-06
“International trade as the sole engine of growth for an economy”
(Juny 2009)

XREAP2009-07
Callejón, M. (PPRE-IREA), Ortún V, M.
“The Black Box of Business Dynamics”
(Setembre 2009)

XREAP2009-08
Lucena, A. (CREB)
“The antecedents and innovation consequences of organizational search: empirical evidence for Spain”
(Octubre 2009)

XREAP2009-09
Domènech Campmajó, L. (PPRE-IREA)
“Competition between TV Platforms”
(Octubre 2009)
XREAP2009-10
Solé-Auró, A. (RFA-IREA), Guillén, M. (RFA-IREA), Crimmins, E. M.
“Health care utilization among immigrants and native-born populations in 11 European countries. Results from the Survey of Health, Ageing and Retirement in Europe”
(Octubre 2009)

XREAP2009-11
Segarra, A. (GRIT), Teruel, M. (GRIT)
“Small firms, growth and financial constraints”
(Octubre 2009)

XREAP2009-12
Matas, A. (GEAP), Raymond, J.LL (GEAP), Ruiz, A. (GEAP)
“Traffic forecasts under uncertainty and capacity constraints”
(Novembre 2009)

XREAP2009-13
Sole-Ollé, A. (IEB)
“Inter-regional redistribution through infrastructure investment: tactical or programmatic?”
(Novembre 2009)

XREAP2009-14
Del Barrio-Castro, T., García-Quevedo, J. (IEB)
“The determinants of university patenting: Do incentives matter?”
(Novembre 2009)

XREAP2009-15
Ramos, R. (AQR-IREA), Suriñach, J. (AQR-IREA), Artís, M. (AQR-IREA)
“Human capital spillovers, productivity and regional convergence in Spain”
(Novembre 2009)

XREAP2009-16
Álvarez-Albelo, C. D. (CREB), Hernández-Martín, R.
“The commons and anti-commons problems in the tourism economy”
(Desembre 2009)
2010

XREAP2010-01
García-López, M. A. (GEAP)
“The Accessibility City. When Transport Infrastructure Matters in Urban Spatial Structure”
(Febrer 2010)

XREAP2010-02
García-Quevedo, J. (IEB), Mas-Verdú, F. (IEB), Polo-Otero, J. (IEB)
“Which firms want PhDs? The effect of the university-industry relationship on the PhD labour market”
(Març 2010)

XREAP2010-03
Pitt, D., Guillén, M. (RFA-IREA)
“An introduction to parametric and non-parametric models for bivariate positive insurance claim severity distributions”
(Març 2010)

XREAP2010-04
Bermúdez, Ll. (RFA-IREA), Karlis, D.
“Modelling dependence in a ratemaking procedure with multivariate Poisson regression models”
(Abril 2010)

XREAP2010-05
Di Paolo, A. (IEB)
“Parental education and family characteristics: educational opportunities across cohorts in Italy and Spain”
(Maig 2010)

XREAP2010-06
Simón, H. (IEB), Ramos, R. (AQR-IREA), Sanromá, E. (IEB)
“Movilidad ocupacional de los inmigrantes en una economía de bajas cualificaciones. El caso de España”
(Juny 2010)

XREAP2010-07
Di Paolo, A. (GEAP & IEB), Raymond, J. Ll. (GEAP & IEB)
“Language knowledge and earnings in Catalonia”
(Juliol 2010)

XREAP2010-08
“Prediction of the economic cost of individual long-term care in the Spanish population”
(Setembre 2010)

XREAP2010-09
Di Paolo, A. (GEAP & IEB)
“Knowledge of catalan, public/private sector choice and earnings: Evidence from a double sample selection model”
(Setembre 2010)
XREAP2010-10
Coad, A., Segarra, A. (GRIT), Teruel, M. (GRIT)
“Like milk or wine: Does firm performance improve with age?”
(Setembre 2010)

XREAP2010-11
Di Paolo, A. (GEAP & IEB), Raymond, J. Ll. (GEAP & IEB), Calero, J. (IEB)
“Exploring educational mobility in Europe”
(Octubre 2010)

XREAP2010-12
Borrell, A. (GiM-IREA), Fernández-Villadangos, L. (GiM-IREA)
“Clustering or scattering: the underlying reason for regulating distance among retail outlets”
(Desembre 2010)

XREAP2010-13
Di Paolo, A. (GEAP & IEB)
“School composition effects in Spain”
(Desembre 2010)

XREAP2010-14
Fageda, X. (GiM-IREA), Flores-Fillol, R.
“Technology, Business Models and Network Structure in the Airline Industry”
(Desembre 2010)

XREAP2010-15
Albalate, D. (GiM-IREA), Bel, G. (GiM-IREA), Fageda, X. (GiM-IREA)
“Is it Redistribution or Centralization? On the Determinants of Government Investment in Infrastructure”
(Desembre 2010)

XREAP2010-16
Oppedisano, V., Turati, G.
“What are the causes of educational inequalities and of their evolution over time in Europe? Evidence from PISA”
(Desembre 2010)

XREAP2010-17
Canova, L., Vaglio, A.
“Why do educated mothers matter? A model of parental help”
(Desembre 2010)
XREAP2011-01
Fageda, X. (GiM-IREA), Perdiguero, J. (GiM-IREA)
“An empirical analysis of a merger between a network and low-cost airlines”
(Maig 2011)

XREAP2011-02
Moreno-Torres, I. (ACCO, CRES & GiM-IREA)
“What if there was a stronger pharmaceutical price competition in Spain? When regulation has a similar effect to collusion”
(Maig 2011)

XREAP2011-03
Miguélez, E. (AQR-IREA); Gómez-Miguélez, I.
“Singling out individual inventors from patent data”
(Maig 2011)

XREAP2011-04
Moreno-Torres, I. (ACCO, CRES & GiM-IREA)
“Generic drugs in Spain: price competition vs. moral hazard”
(Maig 2011)

XREAP2011-05
Nieto, S. (AQR-IREA), Ramos, R. (AQR-IREA)
“¿Afecta la sobreeducación de los padres al rendimiento académico de sus hijos?”
(Maig 2011)

XREAP2011-06
Pitt, D., Guillén, M. (RFA-IREA), Bolancé, C. (RFA-IREA)
“Estimation of Parametric and Nonparametric Models for Univariate Claim Severity Distributions - an approach using R”
(Juny 2011)

XREAP2011-07
Guillén, M. (RFA-IREA), Comas-Herrera, A.
“How much risk is mitigated by LTC Insurance? A case study of the public system in Spain”
(Juny 2011)

XREAP2011-08
Ayuso, M. (RFA-IREA), Guillén, M. (RFA-IREA), Bolancé, C. (RFA-IREA)
“Loss risk through fraud in car insurance”
(Juny 2011)

XREAP2011-09
Duch-Brown, N. (IEB), García-Quevedo, J. (IEB), Montolio, D. (IEB)
“The link between public support and private R&D effort: What is the optimal subsidy?”
(Juny 2011)
XREAP2011-10
Bermúdez, L.I. (RFA-IREA), Karlis, D.
“Mixture of bivariate Poisson regression models with an application to insurance”
(Juliol 2011)

XREAP2011-11
Varela-Irimia, X-L. (GRIT)
“Age effects, unobserved characteristics and hedonic price indexes: The Spanish car market in the 1990s”
(Agost 2011)

XREAP2011-12
Bermúdez, L.I. (RFA-IREA), Ferri, A. (RFA-IREA), Guillén, M. (RFA-IREA)
“A correlation sensitivity analysis of non-life underwriting risk in solvency capital requirement estimation”
(Setembre 2011)

XREAP2011-13
“A logistic regression approach to estimating customer profit loss due to lapses in insurance”
(Octubre 2011)

XREAP2011-14
Jiménez, J. L., Perdiguero, J. (GiM-IREA), García, C.
“Evaluation of subsidies programs to sell green cars: Impact on prices, quantities and efficiency”
(Octubre 2011)

XREAP2011-15
Arespa, M. (CREB)
“A New Open Economy Macroeconomic Model with Endogenous Portfolio Diversification and Firms Entry”
(Octubre 2011)

XREAP2011-16
Matas, A. (GEAP), Raymond, J. L. (GEAP), Roig, J.L. (GEAP)
“The impact of agglomeration effects and accessibility on wages”
(Novembre 2011)

XREAP2011-17
Segarra, A. (GRIT)
“R&D cooperation between Spanish firms and scientific partners: what is the role of tertiary education?”
(Novembre 2011)

XREAP2011-18
García-Pérez, J. I.; Hidalgo-Hidalgo, M.; Robles-Zurita, J. A.
“Does grade retention affect achievement? Some evidence from PISA”
(Novembre 2011)

XREAP2011-19
Arespa, M. (CREB)
“Macroeconomics of extensive margins: a simple model”
(Novembre 2011)
XREAP2011-20
García-Quevedo, J. (IEB), Pellegrino, G. (IEB), Vivarelli, M.
“The determinants of YICs’ R&D activity”
(Desembre 2011)

XREAP2011-21
González-Val, R. (IEB), Olmo, J.
“Growth in a Cross-Section of Cities: Location, Increasing Returns or Random Growth?”
(Desembre 2011)

XREAP2011-22
Gombau, V. (GRIT), Segarra, A. (GRIT)
“The Innovation and Imitation Dichotomy in Spanish firms: do absorptive capacity and the technological frontier matter?”
(Desembre 2011)
XREP2012-01
Borrell, J. R. (GiM-IREA), Jiménez, J. L., García, C.
“Evaluating Antitrust Leniency Programs”
(Gener 2012)

XREP2012-02
Ferri, A. (RFA-IREA), Guillén, M. (RFA-IREA), Bermúdez, Ll. (RFA-IREA)
“Solvency capital estimation and risk measures”
(Gener 2012)