

Additional file 1 – Equalities (2) and (3)

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Derivation of equalities (2) and (3).

When defining the boundaries of a given probability interval we require that the differences of all expression values are within a constant number of standard deviations, i.e. for any values Y_1 and Y_2 we have a condition

$$-K_{\alpha}SD < Y_2 - Y_1 < K_{\alpha}SD. \quad (\text{A1})$$

Using the condition (A1) we can express the upper limit of Y_2 in terms of Y_1 as

$$Y_U = K_{\alpha}SD + Y_1. \quad (\text{A2})$$

Substituting for SD the expression

$$SD = a_1 + a_2 \frac{Y_1 + Y_2}{2} \quad (\text{A3})$$

we obtain

$$Y_U = K_{\alpha}a_1 + Y_1 + \frac{K_{\alpha}}{2}a_2(Y_1 + Y_{2U}) \quad (\text{A4})$$

and subsequently

$$Y_U = \frac{Y_1 + K_{\alpha}(a_1 + a_2Y_1/2)}{1 - K_{\alpha}a_2/2}. \quad (\text{A5})$$

Similarly for the lower limit we write

$$Y_L = K_{\alpha}SD + Y_1 \quad (\text{A6})$$

and, finally,

$$Y_L = \frac{Y_1 - K_{\alpha}(a_1 + a_2Y_1/2)}{1 + K_{\alpha}a_2/2}. \quad (\text{A7})$$