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Tunneling magnetoresistance phenomenon utilizing graphene magnet electrode

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Using magnetic rare-metals for spintronic devices is facing serious problems for the environmental contamination and the limited material-resource. In contrast, by fabricating ferromagnetic graphene nanopore arrays (FGNPAs) consisting of honeycomb-like array of hexagonal nanopores with hydrogen-terminated zigzag-type atomic structure edges, we reported observation of polarized electron spins spontaneously driven from the pore edge states, resulting in rare-metal-free flat-energy-band ferromagnetism. Here, we demonstrate observation of tunneling magnetoresistance (TMR) behaviors on the junction of cobalt/SiO₂/FGNPA electrode, serving as a prototype structure for future rare-metal free TMR devices using magnetic graphene electrodes. Gradual change in TMR ratios is observed across zero-magnetic field, arising from specified alignment between pore-edge- and cobalt-spins. The TMR ratios can be controlled by applying back-gate voltage and by modulating interpore distance. Annealing the SiO₂/FGNPA junction also drastically enhances TMR ratios up to ~100%. © 2014 AIP Publishing LLC. [<http://dx.doi.org/10.1063/1.4901279>]

Several key components of spintronics have been realized in recent years, e.g., giant magnetoresistance (GMR), tunneling MR (TMR), and spin valve devices.^{1–3} Giant TMR ratios, $(R_{AP} - R_P)/R_P$, where AP and P refer to antiparallel and parallel orientations of the spin configurations of the two electrodes, of ~1000% have been obtained in CoFeB/MgO/CoFeB junctions. A wide variety of materials have been utilized for spintronic devices such as ferromagnetic metals and^{1–3} ferromagnetic semiconductors.^{4–6} In all cases, however, rare magnetic elements are essential to provide polarized spins to the systems.

In contrast, it was theoretically predicted that graphene edges with specified atomic structures (the so-called zigzag edge, Fig. 1(b)) are spontaneously spin polarized, exhibiting flat-energy-band ferromagnetism caused from extremely high electronic density of spin states (i.e., the edge states) and a strong spin interaction among the localized electrons.^{7–9} Importantly, this occurs despite the absence of rare magnetic elements, considering just carbon atoms with sp^2 orbitals. In the case of graphene nanoribbons (GNR, Fig. 1(b)),^{7,10} the appearance of the spin polarization is highly sensitive to the spin interaction between the two edges and is determined so as to maximize exchange energy gain (similar to Hund's rule in atoms). In particular, spin ground states in GNRs under absent magnetic fields are still under debating stages. These properties suggest that novel types of spin-based devices may be realized using graphene-based materials, without the need

of rare magnetic atoms. Long spin diffusion lengths and the introduction of the spin-orbit interaction by hydrogenation^{11,12} are further recent examples of the potential of graphene spintronics.

In prior works, we have experimentally confirmed the formation of this flat-band ferromagnetism in hydrogen (H)-terminated zigzag-edged GNPAs (Figs. 1(a) and 1(b)).^{13–16} Because the GNPAs corresponds to a large ensemble of the zigzag GNRs (i.e., interpore regions), it is effective to detect small magnetic and electric signals arising from the pore edge spins. Observation of the significant reduction of the G/D peak ratios by the critical-temperature annealing (~800 °C) in Raman spectrum and the comparison with the previous other experiments (e.g., extremely low G/D peak ratios in the intentionally fabricated zigzag-edge hexagonal pores¹⁷ and in the zigzag-edged graphene flakes,¹⁸ atomic reconstruction to zigzag edge by Joule heating,¹⁹ and electron beam irradiation²⁰) implied the formation of the zigzag-type atomic structure of the pore edges by the reconstruction of the edge atomic structure. Moreover, observation of the ferromagnetism induced by decreasing the interpore distance and of the high density of the polarized spins at the pore edges by magnetic force microscope in the ferromagnetic graphene nanopore arrays (FGNPAs)^{13,14} suggested that the observed ferromagnetism was attributed to the presence of the polarized spins existing at the pore edges. Two theoretical analysis (GNR theory and Lieb's theorem^{21,22}) of the observed magnetization values (~0.3 μ_B /edge dangling bond) also suggested that the mono-hydrogenated zigzag pore edges were the origin for the ferromagnetism.^{13,15} Recent our work has proved

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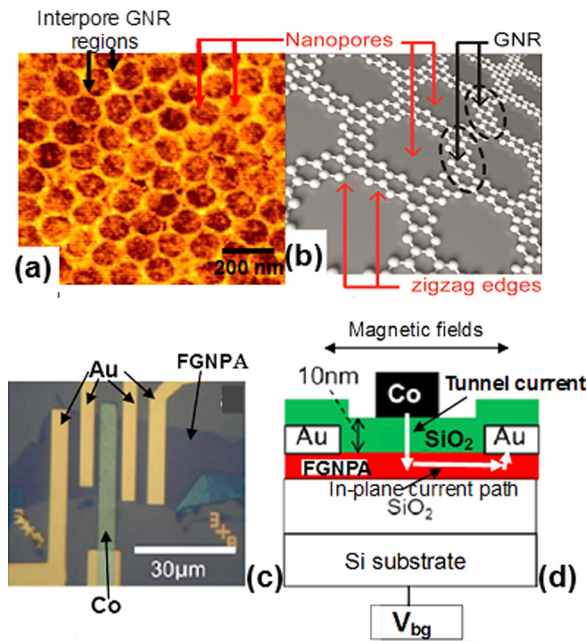


FIG. 1. (a) AFM image of the FGMPA, which consists of a honeycomb-like array of hexagonal nanopores. The typical inter-pore distance is ~ 30 nm and the pore diameter is ~ 80 nm. (b) Schematic top view of a GMPA with zigzag-type atomic structure at the pore edges. Inter-pore regions correspond to zigzag-type GNRs (e.g., with width of ~ 30 nm), which are one-dimensional strip lines of graphenes. In actual samples, larger number of carbon unit cells exists in one inter-pore-GNR region. (c) Optical microscope image of a top view of the electrode pattern of the Co/SiO₂/FGMPA TMR junction. MR between the top Co electrode and the Au electrode located at the nearest right side was measured under constant current mode of 1 nA. (d) Schematic cross section of the TMR junction. The white line illustrates the constant current path. Thickness of the SiO₂ tunnel barrier of ~ 10 nm was confirmed by ellipsometry. Magnetic fields were applied in parallel with the FGMPA plane. A back gate voltage (V_{bg}) was applied from the back side of the Si substrate via surface SiO₂ film of Si substrate.

this by increasing saturation magnetization in mostly 100 times by increasing area of mono-hydrogen termination of the pore edges using specified resist treatment.¹⁵ The edge states were also confirmed by observation using ionic liquid gate.¹⁶ Also from other viewpoints, GMPAs are highly expected as quantum-information,²³ optical,²⁴ and semiconducting-operation²⁵ devices.

In the present study, TMR junctions utilizing such FGMPAs as ferromagnetic electrodes are realized. The fabricated TMR junction consists of Co/SiO₂/FGMPA (Figs. 1(c) and 1(d)), serving as a prototype structure for rare-metal free graphene-based TMR. The honeycomb-like array of hexagonal nanopores forming the FGMPA is shown in the atomic force microscope image (Fig. 1(a)) and in a schematic view (Fig. 1(b)). Fabrication followed our previous non-lithographic method,^{13–16} which realized the low defects and low contamination of the zigzag pore edges.

The fabricated TMR structure using this FGMPA as one-side electrode with the optical microscope is shown in Fig. 1(c) (top-view) and is schematically described in Fig. 1(d). The TMR behavior is measured along the constant current path illustrated in Fig. 1(d). The TMR ratio is defined as the difference between the resistance values (R_B) at individual magnetic fields (B) and the minimum MR value (R_{min}), which is assumed to be the best parallel spin alignment between Co electrode and FGMPA; i.e., TMR ratio = $(R_B - R_{min})/R_{min}$. A

magnetization measurement of the overlaid structure of the SiO₂/FGMPA implies the persistence of the ferromagnetic signal even after evaporation of the SiO₂ film on the pore edges, although the magnitude is reduced somewhat compared with that without SiO₂ film.

Figures 2(a) and 2(b) give the result of a typical TMR measurement of the Co/SiO₂/FGMPA junction (shown in Figs. 1(c) and 1(d)) under in-plane parallel B at (a) 1.5 K and (b) 300 K. We identify the minimum resistance (R_{min}) as the situation in which the external B induces best matching between the spin polarizations of the magnetic materials (i.e., parallel spin alignment between cobalt and FGMPA) and take this as R_P in subsequent calculations of TMR ratios, as mentioned in the figure caption. The observed TMR behaviors in Fig. 2(a) are significantly different from those of any other conventional TMR junctions. They exhibit the following unique B -dependent characteristics. (1) TMR ratio is tuned by the B and can reach a signal about 20%. (2) The minimum of TMR ratio appears as B approaches to zero in $-B$ region. (3) The TMR ratios increases gradually crossing $B = 0$. (4) The peak of TMR ratio emerges in $+B$ region. A similar behavior is observed for polarity changes in B , i.e., when sweeping from $+B$ to $-B$ (the black line in Fig. 2). As illustrated in the curves around zero-TMR ratio, the Co/SiO₂/bulk graphene junction (i.e., without the nanopores) shows drastically different behavior, with showing no clear TMR signatures. This suggests that the TMR-like behavior

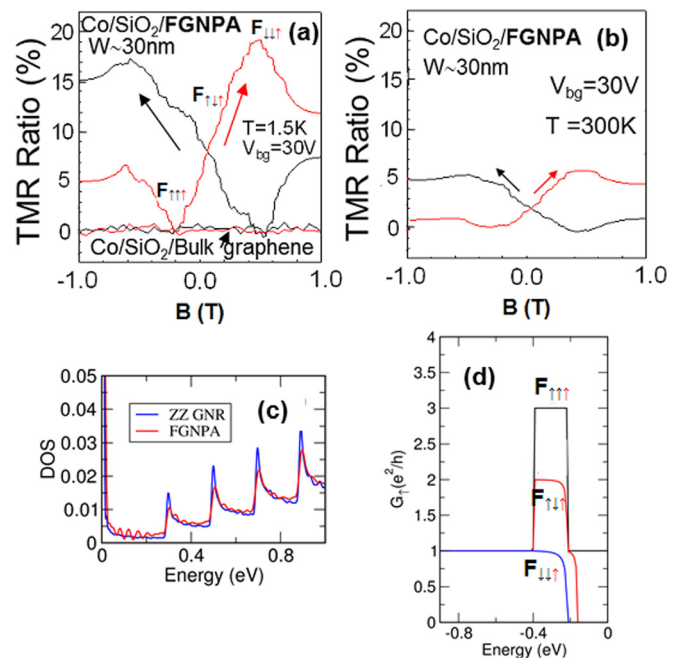


FIG. 2. The result of a typical TMR measurement of the Co/SiO₂/FGMPA junction (shown in Figs. 1(c) and 1(d)) under in-plane parallel B at (a) 1.5 K and (b) 300 K. In-plane magnetic field sweeps were performed from $B = -1$ to $+1$ T (red line) and $B = +1$ to -1 T (black line). Mostly constant zero TMR ratios shown in (a) are TMR values for the bulk graphene/SiO₂/Co junction. Notation $F_{\uparrow\uparrow}$ means spin configuration of the two edges of an inter-pore GNR region in the FGMPAs (left two black-arrows) and the Co (right one red-arrow). (c) Density of states calculated for the GMPA with an inter-pore distance of $W \sim 10$ nm and a pore diameter of ~ 80 nm and the related zigzag GNR. (d) Conductance between zigzag GNR junctions with different edge spin polarization states and cobalt electrode. Note the distinct differences in the MR signal in the energy regime where edge states dominate the electronic properties of the GNR.

observed in the Co/SiO₂/FGNPA junction is unique to the present TMR structure, and is driven by spin tunneling properties between the Co electrode and the FGNPA. Present reproducibility of the TMR behaviors is over 80%, because six of seven samples showed similar behaviors to date.

TMR properties observed at room temperature are shown in Fig. 2(b). Maximum TMR ratios decrease from ~20% to ~5% owing to the reduced flat-band ferromagnetism and the behaviors become much ambiguous compared with those at low temperatures, showing non-zero TMR ratios at high B due to thermal spin instability. It should be noticed that, nevertheless, TMR behaviors are still observable.

The observed unique TMR behavior can be qualitatively understood by considering the spin alignment between two opposing pore edges of the FGNPA (i.e., two edges of the interpore GNR region in Fig. 1(b)) and the Co electrode. It also clarifies spin ground states of the H-terminated zigzag-type GNRs under no B . We support these interpretations by atomistic simulations. First, we calculate the density of states (DOS) of a GNP reminiscent of the fabricated structure. The calculated DOS (Fig. 2(c)) is compared to that obtained for an infinitely long zigzag GNR (i.e., interpore GNR region in Fig. 1(b)). Ignoring the tunnel barrier, the TMR device is thus conveniently visualized as a junction between a Co spin injector and an array of uncoupled zigzag GNRs, the spin polarizations of which depend on the B . Based on this result, we simulate the spin transport properties of the device via a zigzag GNR-based junction, in which the spin polarization is differentiated between left (Co spin injector) and right (FGNPA) parts (Fig. 3(d)). We focus on the sweep from $-B$ to $+B$ (red curve in Fig. 2(a)).

As indicated in Fig. 2(d), we identify three distinct regions in the TMR response, corresponding to the situations where the magnetization of the FGNPA (i.e., spin alignment of two edges of the interpore GNRs) is ferromagnetic ($F_{\uparrow\uparrow}$: the left

two black arrows at the subscript in the figure mean the spin moment of two edges of the interpore GNR) with spins parallel to the spin injector (Co) ($F_{\uparrow\uparrow}$: the right one red subscript arrow in the figure is the spin moment of injector), anti-ferromagnetic (AF, $F_{\uparrow\downarrow}$), and ferromagnetic with spins anti-parallel to the spin injector ($F_{\downarrow\downarrow}$). At $-B$, the spins of the injector and the FGNPA are largely parallel ($F_{\uparrow\uparrow}$), resulting in maximum conductance through the junction (Fig. 2(d)) and thus the minimum of the TMR ratio in Fig. 2(a). As the B approaches zero, the GNR array (i.e., ensemble of the two edges of the interpore GNRs) gradually transitions to an AF configuration ($F_{\uparrow\downarrow}$), where half of the conductance channels are suppressed, resulting in the half value of conductance (Fig. 2(d)) and gradual increase in the TMR ratio ($F_{\uparrow\uparrow}$). As the B is increased further to $+B$, the spin polarization of the GNR array changes to the ($F_{\downarrow\downarrow}$) configuration, suppressing all edge conductance channels, resulting in the conductance minimum (Fig. 2(d)) and subsequent the peak of TMR ratio observed around $B = 0.5$ T ($F_{\downarrow\downarrow}$). These calculations suggest that gradual changes in TMR ratios can be actually possible. At higher $+B$, the spins of the Co injector start to align with the magnetic field, gradually quenching the TMR ratio, while non-zero TMR ratios in higher $+B$ regions suggest instability of the pore edge spins of the FGNPAs as well as those in $-B$ region.

It implies that the edge polarized spins of the interpore GNR regions can actually tunnel through SiO₂ barrier forming the spin alignment with the spins of Co electrode and also that the spin ground states of the H-terminated zigzag GNRs are AF under no B . This result is consistent with our previous experimental results, which exhibited ferromagnetism only when B is applied.^{13,14} It is important to note that the main mechanism revealed by our simulations does not depend on how the electrons are really injected from the cobalt electrode to the GNP, but how efficiently spin-polarized electrons injected on the GNP are further transmitted depending on the magnetic ordering of the local moments along the zigzag edges.

Here, we also demonstrate that the TMR characteristics can be controlled by changing a back gate voltage (V_{bg} : Fig. 1(d)) (Figs. 3(a) and 3(b)), as well as to the interpore spacing (W , i.e., width of interpore GNRs in Fig. 1(b)) (Figs. 3(c) and 3(d)). The TMR ratio exhibits a maximum value of ~20% at $V_{bg} = +30$ V (Figs. 3(a) and 3(b)), while it is reduced with decreasing V_{bg} toward $-V_{bg}$ region. This is consistent with the presence of evident spin-based phenomena observed only at $V_{bg} = +30$ V for previous in-plane MR behaviors of FGNPAs.¹³ This is because the Au electrode was placed at the side position of the Co/SiO₂/FGNPA junction and the in-plane spin current path exists through the H-terminated FGNPA between the TMR junction and the Au electrode in the present specified sample structure (Fig. 1(d)). Although the polarized spins at the pore edges and TMR ratio themselves have basically no correlation with the V_g , the spin current through the in-plane path is significantly reduced with decreasing V_g due to the n-type semiconducting behavior of the interpore GNR regions of the GNP.¹³ This makes TMR features difficult to detect, resulting in the decreases in the observed TMR ratios.

For larger interpore spacing of $W \sim 40$ nm, the TMR value further decreases significantly (Figs. 3(c) and 3(d)).

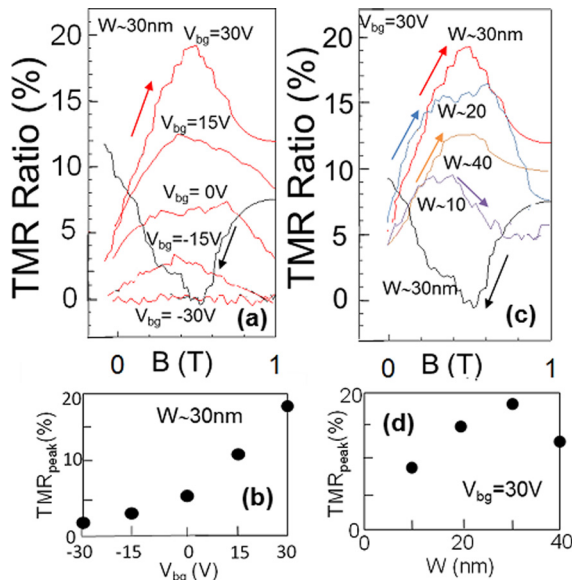


FIG. 3. (a) Measurements of the sample shown in Fig. 2 for V_{bg} from +30 V to -30 V are shown by red curves, while a black line shows that for $-B$ to $+B$ regions for reference. (b) V_{bg} dependence of peak values of the TMR ratios shown in Fig. 3(a). (c) Measurements of a sample similar to that in Fig. 2(a) but with different W . Exhibited B regions are the same as Fig. 3(a). (d) W dependence of peak values of the TMR ratios shown in Fig. 3(c).

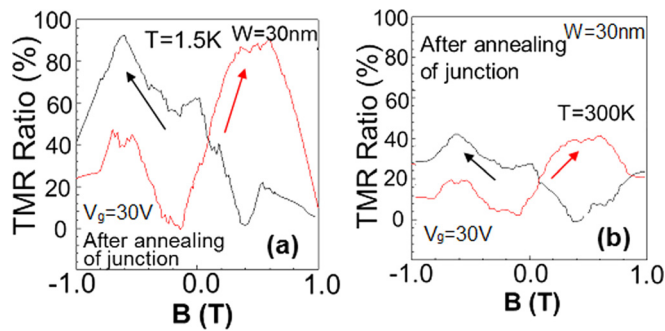


FIG. 4. TMR behaviors of the Co/SiO₂/FGNPA junction improved by annealing at (a) 1.5 K and (b) 300 K. The annealing of SiO₂/FGNPA junction at 500 °C was carried out under high vacuum atmosphere right after depositing of SiO₂ layer on FGNPA.

For such a large spacing, the spin polarization of opposing pore edges (i.e., two edges of interpore GNRs) becomes unstable due to suppressed spin interaction,¹³ quenching the TMR properties. TMR ratios also decrease when using FGNPAs with smaller W (Figs. 3(c) and 3(d)), because $W \leq 20$ nm is too narrow to form spin currents along the in-plane current path through the FGNPA to Au electrode (Fig. 1(d)). Although ferromagnetism is stronger for smaller W ,¹³ induced scattering by the nanopore array heavily obstructs spin flow to the Au electrode, reducing the TMR ratio. This is again consistent with previously observed spin-based phenomena in FGNPAs with $W \sim 30$ nm.¹³ Therefore, the optimum W value exists for the TMR ratios.

We have presented unique TMR behaviors in the Co/SiO₂/FGNPA junctions. Nevertheless, the maximum TMR ratio is as low as $\sim 20\%$ at best (Fig. 2(a)). One of the main reasons is the poor interaction at the lattice-mismatched SiO₂/FGNPA interface, particularly at the H-terminated pore edges, which destructs transport of the spin-alignment current and reduces TMR ratios. In contrast, as shown in Fig. 4(a), we find that annealing of the SiO₂/FGNPA structure at ~ 500 °C right after the deposition of SiO₂ tunneling layer drastically (i.e., ≥ 5 times) improves the TMR ratios of Fig. 2(a), although some instability of the pore edge spins still remain as some irregular small TMR ratio peaks. At room temperature, the maximum TMR ratio increases even by ~ 10 times (Fig. 4(b)) compared to that in Fig. 2(b).

This promises that introducing a lattice-matched tunnel barrier layer (e.g., graphene oxide) instead of SiO₂ layer and also improvement of magnitude of the ferromagnetism in the FGNPAs (e.g., utilizing HSQ resist treatment¹⁵) can increase TMR ratios further and make evident room-temperature operation possible. Moreover, realization of FGNPA/(lattice-matched tunnel barrier)/FGNPA junction must significantly improve the performance of the TMR behaviors toward $\sim 1000\%$ order.

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