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Optical and electronic properties of 2H-MoS₂ under pressure: revealing the spin-polarized nature of bulk electronic bands

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Abstract

Monolayers of transition-metal dichalcogenide semiconductors present spin-valley locked electronic bands, a property with applications in valleytronics and spintronics that is usually believed to be absent in their centrosymmetric (as the bilayer or bulk) counterparts. Here we show that bulk 2H-MoS₂ hides a spin-polarized nature of states determining its direct band gap, with the spin sequence of valence and conduction bands expected for its single layer. This relevant finding is attained by investigating the behavior of the binding energy of A and B excitons under high pressure, by means of absorption measurements and density-functional-theory calculations. These results raise an unusual situation in which bright and dark excitons degeneracy is naturally broken in a centrosymmetric material. Additionally, the phonon-assisted scattering process of excitons has been studied by analyzing the pressure dependence of the linewidth of discrete excitons observed at the absorption coefficient edge of 2H-MoS₂. Also, the pressure dependence of the indirect optical transitions of bulk 2H-MoS₂ has been analyzed by absorption measurements and density-functional-theory calculations. These results reflect a progressive closure of the indirect band gap as pressure increases, indicating that metallization of bulk MoS₂ may occur at pressures higher than 26 GPa.

I. INTRODUCTION

The property that makes monolayers (MLs) of transition-metal dichalcogenide (TMD) semiconductors (such as MoS₂, MoSe₂, WS₂, and WSe₂) unique among two-dimensional (2D) materials is the unusual combination of strong spin-orbit interactions, broken inversion symmetry and time-reversal symmetry [1,2]. The restrictions that they altogether impose can promote that the spin-polarization of degenerate electronic states is reversed between states at ${\bf k}$ and ${\bf -k}$ in these MLs, which makes possible a selective photoexcitation of carriers in the K and K' valleys by using left or right circularly polarized light, respectively [1,3], as well as the observation of the valley Hall effect [4] and the realization of polarization-sensitive polaritonic devices operating at room temperature [5]. Collaterally, this particular property of these 2D materials has sowed the seeds for the search of new kind of 2D ferroic systems [6], Weyl fermions [7] and topological superconductors [8]. Also, potential spintronic applications of 2D TMDs are very promising [9,10]. Spin splitting between the two highest valence bands at the K point (Δ_V) are known to be hundreds of meV [1-3]. However, for spintronic applications based on n-type 2D TMDs, it would be required a precise knowledge of the spin-polarization degree of their conduction bands and relatively large conduction-band spin-splitting (Δ_c) values. In this sense, a precise determination of Δ_c is also relevant to elucidate the dark/bright nature of excitons in 2D TMDs [11-14], which plays an important role in exciton lifetimes and quantum efficiencies for optical recombination processes [15-17]. Only recently, experimental studies on the spin-sequence of conduction bands and ∆c values have been reported for MLs of WSe2, MoSe2, and MoS2 [18–20], giving results consistent with calculations [12,21,22].

It is usually believed that the spin-polarization of the electronic bands of TMDs naturally emerges, only, in 2D TMDs with an odd number of layers and that it is absent in 2H-MoS₂ [23]. However, it has been suggested that hidden forms of spin-polarization can exist even in centrosymmetric crystals under the condition that the spin-polarized bands are spatially localized apart from each other [24,25]. This interesting possibility would open the door to explore technological implications of the spin-polarized nature of TMDs not only in MLs but also in bilayers or bulk forms. Spin-polarized and angle-resolved photoemission techniques have provided for a direct evidence of the existence of a hidden spin texture in the valence bands of centrosymmetric

WSe₂ [26] and in 2H-MoS₂ by using left- and right-handed circularly polarized light [27]. However, photoemission is a surface-sensitive technique that mostly probes the outermost layer, in which the inversion symmetry is broken and the interlayer effects are partly removed.

In this work, we have studied the optical and electronic properties of 2H-MoS₂ by optical absorption measurements under high pressure and density functional theory (DFT) calculations. This study has allowed us to approach the question of the hidden spin-polarized nature of the bulk valence and conduction bands. By applying pressure, we experimentally and theoretically demonstrate that the pressure dependence of the excitonic optical transitions (specifically, the exciton binding energy) can be only understood by considering that the two highest valence bands and the two lowest conduction bands at the K(K') points are spin-polarized, with a spin sequence that agrees with that expected by calculations reported so far for its ML. Moreover, our results evidence that the hidden spin-polarized nature of 2H-MoS₂ also conveys the rarely observed lift of the degeneracy between bright and dark excitons in a centrosymmetric material. Besides, relevant questions related to the phonon-assisted scattering process for A and B excitons and the evolution of the indirect band gap (Eg^{ind}) of bulk 2H-MoS₂ under pressure, have been also approached.

II. SPIN-VALLEY POLARIZATION OF ELECTRONIC BANDS OF 2H-MoS₂

A. Pressure dependence of optical absorption coefficient of 2H-MoS₂

High-pressure techniques are particularly efficient in tuning the strength of interlayer interactions and elucidating their effects on the electronic and optical properties of layered materials [28]. In fact, from the point of view of the interlayer interactions in layered materials, high-pressure and exfoliation techniques are two sides of the same coin. The fundamental optical absorption edge of 2H-MoS₂ has been measured in a 0.13 μm thick sample under different hydrostatic pressure conditions, ranging between ambient pressure and 13 GPa [Fig. 1(a)). The two well established A and B direct excitonic transitions of MoS₂ are clearly observed at ambient pressure [29,30], as well as a high-energy tail labeled as C that has been attributed to high-energy transitions occurring between states located at midpoint along the ΓK high-symmetry

direction [31,32]. As pressure increases, the A and B excitonic peaks blueshift and broaden, being no longer observable at pressures higher than 10 and 8 GPa, respectively, whereas the C-feature redshifts with no remarkable changes in shape. Upon decreasing pressure (top spectrum in Fig. 1(a)) the excitonic peaks are fully recovered, indicating that pressure-induced defects are not responsible for the disappearance of the excitonic peaks observed at high pressure. The absorption coefficient spectra showed in Fig. 1(a) have been analyzed in the frame of the Elliott-Toyozawa model [33,34] for a direct absorption including electron-hole interaction and considering a Gaussian broadening of the direct exciton line shapes due to the strong electron-phonon interaction in MoS_2 [35]. This model has been largely employed in literature to successfully describe the optical absorption edge of diamond or zinc-blende [36–38] and layered [39–42] semiconductors as well as 2D quantum-well systems [43,44]. In the frame of Elliott-Toyozawa model [33,34], the absorption coefficient (α_{E-T}) can be expressed as

$$\alpha_{E-T}(E) = \frac{c_{0A}R_A^{\frac{1}{2}}}{E} \left\{ \sum_{m=1}^{\infty} \frac{2R_A}{m^3} \frac{1}{\sigma_{mA}\sqrt{2\pi}} e^{-\frac{(E-E_{mA})^2}{2\sigma_{mA}^2}} + \int_{E_{0A}}^{\infty} dE' \frac{1}{1-e^{-2\pi\sqrt{\frac{R_A}{E'-E_{0A}}}}} \frac{1}{\sigma_{c,A}\sqrt{2\pi}} e^{\frac{(E'-E)^2}{2\sigma_{cA}^2}} \right\} + \frac{c_{0B}R_B^{\frac{1}{2}}}{E} \left\{ \sum_{m=1}^{\infty} \frac{2R_B}{m^3} \frac{1}{\sigma_{mB}\sqrt{2\pi}} e^{-\frac{(E-E_{mB})^2}{2\sigma_{mB}^2}} + \int_{E_{0B}}^{\infty} dE' \frac{1}{1-e^{-2\pi\sqrt{\frac{R_B}{E'-E_{0B}}}}} \frac{1}{\sigma_{cB}\sqrt{2\pi}} e^{\frac{(E'-E)^2}{2\sigma_{cB}^2}} \right\} , \qquad \text{Eq. (1)}$$

where A and B subindices refer to each one of the direct excitonic transitions. The integral terms in Eq. (1) represent the contribution of both excitonic continuum to the absorption coefficient. In Eq. (1), $C_{0A;B}$ are the absorption-strength parameters of the direct excitonic transitions, $R_{A;B}$ are the exciton Rydberg energies, $E_{0A;B}$ are the band-to-band direct transition energies, $E_{mA;B}$ represent the energy of the discrete m-excitonic transitions. The $\sigma_{cA;B}$ and $\sigma_{mA;B}$ variances can be related to the exciton continuum half-widths ($\Gamma_{cA;B} = \sqrt{2\ln 2}\sigma_{cA;B}$) and the half-width of the discrete exciton lines ($\Gamma_{mA;B} = \sqrt{2\ln 2}\sigma_{mA;B}$), respectively. For the $\Gamma_{mA;B}$ of the discrete m-exciton, the empirical relationship $\Gamma_{mA;B} = \Gamma_{cA;B} - (\Gamma_{cA;B} - \Gamma_{1A;B})/m^2$ has been used [45]. In order to account for the contribution to the absorption coefficient of the high-energy tail [the C feature identified in Fig. 1(a)], a Gaussian-broadened step-like function occurring at the energy E_{0C} has been added to

Eq. (1), as a first approximation to the line shape of the C feature. Under these assumptions, the absorption coefficient (α) can be expressed as

$$\alpha(E) = \alpha_{E-T}(E) + \frac{c_{0C}}{1 + e^{(E_{0C} - E)/\Gamma_{CC}}},$$
 Eq. (2)

where C_{0C} is a proportionality constant, and Γ_{CC} is the width of the step-like direct transitions continuum band edge.

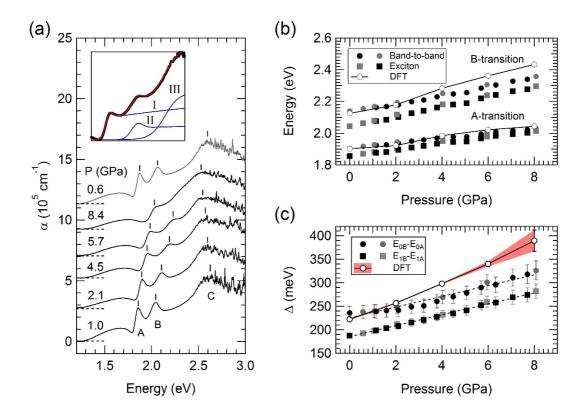


FIG. 1. (a) Fundamental absorption edge of 2H-MoS $_2$ measured under different applied hydrostatic pressures. Evolution with pressure of the identified A, B and C features has been indicated by small solid bars. The inset shows an example of the result of fitting Eq. (2) to the absorption coefficient measured at the selected pressure of 5.07 GPa (red solid line). Each one of the contributions to the fitting curve has been included in the inset (blue solid lines), these corresponding to transitions involving states from the highest (I) and the next (II) valence bands at the K point, as well as these attributable to transitions located around the midpoint of the Γ K high symmetry direction (III). (b) Pressure dependence of the energies of the A and B band-to-band direct transitions ($E_{0A,B}$) and the ground A_1 and B_1 excitonic transitions ($E_{1A,B}$, respectively), as extracted from the fitting of Eq (2) to the experimental results showed in (a). Black and grey symbols represent values obtained in experiments in which hydrostatic pressure increases or decreases, respectively. Error intervals, as extracted from the fitting of Eq. (2) to the experimental data in Fig. 1(a), are smaller than the dimensions of the data points. The pressure dependence of the A and B band-to-band direct transitions, these obtained by DFT calculations, have been included. (c) Pressure dependence of the total band splitting Δ = E_{0B} - E_{0A} at the K point of 2H-MoS $_2$, as obtained from the experimental results collected in (b) (Grey and black points). Error intervals have

been propagated from data shown in (b). White solid points represent the pressure dependence of Δ_v , as obtained by DFT calculations. Since, a priori, optical direct transitions may occur from the two highest valence bands to each one of the two lowest conduction bands at the K point, the pressure dependence of Δ may be expected to evolve between $\Delta_v + |\Delta_c|$ [as would correspond to the MoS₂-like configuration illustrated in Fig. 3(a)] and $\Delta_v - |\Delta_c|$ [i.e., as the WSe₂-like configuration illustrated in Fig. 3(a)]. The range of Δ comprised between these two cases has been indicated by a light-red area and vertical error-like bars, as obtained by DFT. For comparison purposes, the pressure dependence of the difference E_{1B}–E_{1A} has been included in this plot, as extracted from the data showed in (b). Dashed lines are linear fits to the experimental data.

A word should be said about the Gaussian lineshape adopted here to describe the exciton-phonon interaction in Eq (1), in contrast to the Lorentzian one commonly used in high-quality bulk crystals [37–39]. It is commonly accepted that compositional disorder, width fluctuations, and other kinds of disorder, can promote inhomogeneous broadening of excitons, which turn the exciton lineshape into a Gaussian lineshape [44]. Although good-quality MoS₂ crystals have been used in our work, the relatively high binding-energy values of A and B excitons in MoS₂, compared to other non-layered semiconductors, makes the Bohr radius of excitons much lower than these of non-layered semiconductors. Consequently, excitons in 2H-MoS₂ seem to be better described as Frenkel excitons rather than Wannier excitons, and then, with an intrinsic phonon-exciton interaction better described by inhomogeneous broadening, as disorder can promote but extrinsically.

Taking into account these remarks, Equation (2) has been used to analyze the experimental absorption-coefficient curves shown in Fig. 1(a). It should be noticed here that discrete excitonic terms with m>3 have been neglected in these analyses. To conduct further discussion, the inset of Fig. 1(a) illustrates the results of fitting Eq. (2) to the absorption coefficient measured at a selected pressure of 5.07 GPa, in which the different contributions to the fitting curve are detailed. Curves labeled I and II represent the contributions (discrete and continuous) of A and B excitons, respectively. The curve labeled III represents the contribution of the C feature. We would like to stress that, although the absorption coefficient spectrum of 2H-MoS₂ has been measured here for pressures as high as 13 GPa, we have restricted our analysis to range of pressure in which both A and B excitons can be clearly identified and distinguished from the red shifting C-feature (i.e., in the 0-8 GPa). In fact, it can be noticed that, in the absorption coefficient spectrum measured at 8.4 GPa [Fig. 1(a)], only the A exciton can be clearly resolved.

Therefore, proceeding in this way for all the absorption coefficient spectra acquired in the range of 0-8 GPa [Fig. 1(a)], the pressure dependence of some relevant parameters has been obtained. In particular, the E_{0C} , the half-width (Γ_{1A} and Γ_{1B}) and energies (E_{1A} and E_{1B}) of the ground A and B exciton lines, respectively, and the band-to-band direct transition energies E_{0A} and E_{0B} corresponding to the A and B transitions, respectively. In the following subsections, we focus on the analysis of the pressure dependence of the band-to-band and excitonic transitions, whereas results related with the pressure dependence of exciton linewidth and the E_{0C} feature will be discussed later.

B. Pressure dependence of the direct band gap

Unlike the A_1 and B_1 excitons [28,29,46], some lacuna exists for data related to the pressure dependence of band-to-band transitions, especially for these involving the B valence band. From our results (Figure 1(b)), E_{0A} appears to be 1.904 ± 0.005 eV and E_{0B} =2.140 ± 0.010 eV at ambient pressure, in very good agreement with recently reported values [47]. In the range of pressure approached in this study, both E_{0A} and E_{0B} quasi-linearly increase, with pressure coefficients of 15.5 ± 0.4 and 27.2 ± 0.7 meV/GPa respectively. From these results, the pressure dependence of the total band splitting $\Delta = \Delta_c + \Delta_v = E_{0B} - E_{0A}$ can be obtained (Figure 1(c)). A value of $\Delta = 236 \pm 15$ meV is experimentally obtained for 2H-MoS₂ at ambient pressure and in agreement with that obtained by angle-resolved photoemission [48], which evolves with pressure with a quasi-linear pressure coefficient of 11.4 ± 0.6 meV/GPa. These results consistently extend the range of pressures approached by studies reported so far [28,49], providing for a accurate determination of the pressure coefficients of the direct band-to-band transitions of 2H-MoS₂ in a pressure range reaching until 8 GPa.

Results shown in Figs. 1(b) and 1(c) can be understood by considering the tuning of interlayer interactions by means of pressure and their effects on the electronic properties of 2H-MoS₂. Figure 2(a), left side, shows the electronic band structure of bulk MoS₂ calculated at ambient conditions by DFT along the Γ K and the KH high-symmetry directions [see the hexagonal Brillouin zone of 2H-MoS₂ also depicted in Fig. 2(a)], in which spin-orbit coupling has been

included. In line with other calculations reported [50-52], the electronic bands in the vicinity of the direct gap of MoS₂ show (top left and bottom left zoomed plots of Fig. 2(a), for the conduction and valence bands, respectively) two nearly degenerate conduction bands at the K point ($|\Delta_c|=2$ meV at ambient pressure) with different effective masses along the ΓK direction (m*⊥) which are, importantly, strongly localized in the layer plane. With respect to the split valence bands at the K point, it is worth noting that their curvatures have opposite sign along the KH direction. By increasing pressure until 8 GPa, our calculations show that the consequent enhancement of interlayer interactions appears not to alter the orbital nature nor the character of states at the edges of the conduction and valence bands at the K point (Fig. 2(a), middle and right plots), although an unoccupied Mo dxz,yz band [51,53] seems to approach to the bottom of the conduction band as pressure increases. However, it is relevant to notice that the m*_ of the two lowest conduction bands at the K point, as calculated by DFT, evolve with pressure differently from each other (top plots of Fig. 2(a) and Fig. 8 of Appendix B). Besides the effective masses of states involved in the direct optical transitions, other important aspects of the electronic band structure appear to strongly depend on interlayer interactions; specifically, the direct band gap, the total band splitting ($\Delta = \Delta_v + \Delta_c$), and the E_g^{ind} . In spite of the lack of data available in literature regarding the pressure dependence of the E_{0A} and E_{0B} direct transitions, the experimental results obtained [Fig. 1(b)] can be directly contrasted with the electronic band structure of 2H-MoS2 calculated at different pressures [Fig. 2(a)]. The pressure dependence of both E_{0A} and E_{0B}, as obtained by DFT calculations, have been included in Fig. 1(b), which have been rigidly shifted by a constant value of 0.29 eV to take into account the well-known DFT underestimation of the band gap. Apart from this well-known band-gap offset, it appears that the DFT calculations nicely reproduce the pressure dependence of E_{0A} and E_{0B} obtained experimentally. Also, our DFT calculations predict a band splitting of ∆≈∆v=220 meV at ambient pressure, which results from the combination of spin-orbit coupling and interlayer interactions. This value of Δ appears to be in very good agreement with that obtained experimentally [Fig. 1(c)].

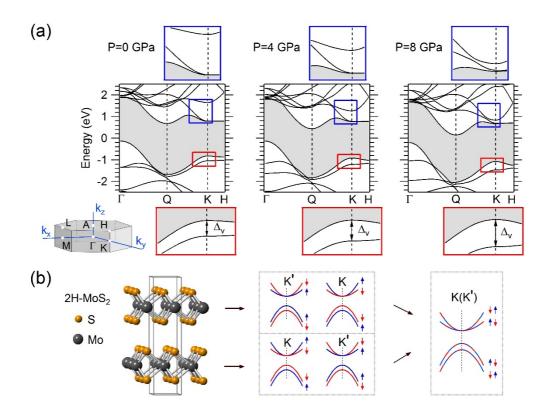


FIG. 2. (a) Electronic band structure of 2H-MoS₂ calculated by DFT along the ΓK and the KH high-symmetry directions of the Brillouin zone (also shown). Calculations have been performed at ambient conditions (left), 4 GPa (center) and 8 GPa (right). The top and bottom panels show zooms of the corresponding electronic conduction and valence bands located in the vicinity of the direct band gap of 2H-MoS₂, respectively. (b) Illustration of the spin-polarized nature of the electronic bands at the K(K') point of each single layer composing the unit cell of 2H-MoS₂ (left side). The characteristics of these bands remain basically unaltered when two layers stack together due to their strongly localized nature, giving rise to energy and spin degenerate bands in the centrosymmetric material that retain spin-information from layer of provenience (right side).

C. Pressure dependence of the A and B excitonic transitions

Let us face now the pressure dependence of the exciton E_{1A} and E_{1B} energies (Figure 1(b)). The energies of the first excitonic transitions result to be E_{1A} = 1.855 ± 0.002 eV and E_{1B} = 2.043 ± 0.002 eV at ambient pressure, following a quasi-linear evolution as pressure increases until 8 GPa with pressure coefficients of 19.6 ± 0.5 and 31.2 ± 0.6 meV/GPa, that nicely agrees with early [54] and recent observations [28]. From these results, the difference in energy between the ground B and A excitonic transitions (E_{1B} - E_{1A}) has been obtained (Figure 1(c)). In MLs of MoS₂, this difference is usually adopted to estimate Δ_{V} ($\approx \Delta$). However, this approach is valid only

if the binding energies of excitons A and B (BE_{1A} and BE_{1B}, respectively) are exactly the same, which is clearly not the case in bulk 2H-MoS₂ [28]. The E_{1B} - E_{1A} difference can be expressed in terms of Δ , BE_{1A}, and BE_{1B} as E_{1B} - E_{1A} = Δ - (BE_{1B} - BE_{1A}). Consequently, the fact that Δ and E_{1B} - E1A [Fig. 1(c)] give different values at each pressure and that they exhibit a different pressure dependence clearly indicates that A and B excitons have a different anisotropic degree and/or different exciton effective masses. This observation will play a key role to unravel, by means of optical absorption measurements, the possible hidden spin-polarized nature of bulk electronic bands at the K point of 2H-MoS₂ [24–27] DFT calculations predict (See Fig. 9 of Appendix C) a finite entanglement between spin, valley and layer index at ambient pressure [24,25], for all valence and conduction states in the vicinity of the K point of 2H-MoS₂. Such a particular spinvalley-index connection has been illustrated in Fig. 2(b): The electronic band structure of centrosymmetric TMDs remains, indeed, spin degenerate even in the presence of spin-orbit coupling. However, since the spin-orbit interaction does not couple orbitals of different layers [25], each single band of the bulk would be expected to preserve the spin and valley index of the atomic layer of provenience. Experimentally, optical absorption arises as a powerful technique to indirectly probe the possible spin-polarized nature of the bulk bands at the K point of 2H-MoS₂ since, in this material, direct optical absorption transitions are, in essence, intralayer processes. This is based on the fact that, although wave functions of states determining the two highest valence bands at the K point exhibit some delocalization along the KH direction, the two lowest conduction bands are strongly localized in the layer plane (see Fig. 2(a) and Fig. 9 of Appendix C). Consequently, the overlap between the Bloch wave functions of initial and final states required for optical absorption processes is spatially limited within each atomic layer. Moreover, as optical absorption techniques involve valence and conduction bands, the possible spin-polarized nature scheme described above appears to be naturally linked to the spin-band sequence of valence and conduction bands at the K point in 2D MoS₂ [12,19,21,22]. In a spin-degenerate case, two optically allowed (spin conserving) direct absorption processes may be expected to occur between each one of the valence bands and the two conduction bands at the K point of 2H-MoS₂ (Figure 2(b), right side). However, in the case that bulk valence and conduction bands retained the spin polarization of their ML constituents [12,21,22], only one of the two mutually exclusive possibilities indicated in Fig. 3(a) could take place, which correspond, each one of these

possibilities, to direct optical transitions attending a spin-band sequence in a WSe₂-like or in a MoS₂-like fashion [12,19–22]. Figure 3(b) shows the pressure dependence of the BE of excitons, as extracted from the results shown in Fig. 1(b). At ambient pressure, the BE of excitons is found to be BE_{1A} = 49 \pm 7 meV and BE_{1B} = 97 \pm 10 meV, which again agree with previous observations [30,53,55,56]. However, to our knowledge, this is the first experimental determination of the BE of both excitons as a function of pressure. Taking into account that the band dispersion of valence and conduction bands along the Γ K and KH high-symmetry directions are all highly anisotropic [Fig. 2(a)], a Gerlach-Pollmann model of an exciton has been adopted [57], in which the anisotropy parameter (β) is defined as

$$\beta = 1 - \frac{\mu_{\perp} \varepsilon_{\perp}(0)}{\mu_{\parallel} \varepsilon_{\parallel}(0)},\tag{3}$$

where μ_{\perp} and μ_{\parallel} are the exciton reduced mass and $\epsilon_{\perp}(0)$, and $\epsilon_{\parallel}(0)$ are the static dielectric constant; both variables particularized for the perpendicular and parallel to the c-axis directions, respectively. In the isotropic case, β = 0 and β < 0 in bulk layered semiconductors such as InSe [58] or GaSe [45]. In the frame of this model, the BE of ground excitons can be written as

$$BE_1 = Ry \frac{\mu_\perp}{\varepsilon_\perp(0)\varepsilon_\parallel(0)} [Z_{00}(\beta)]^2 \tag{4}$$

where Ry = 13.6 eV is the free-exciton Rydberg energy and the $Z_{00}(\beta)$ function is

$$Z_{00}(\beta) = \frac{1}{\sqrt{\beta}} \arcsin \sqrt{\beta} \qquad \text{for } \beta > 0$$

$$Z_{00}(\beta) = 1 \qquad \text{for } \beta = 0$$

$$Z_{00}(\beta) = \frac{1}{\sqrt{|\beta|}} \arcsin h \sqrt{|\beta|} \qquad \text{for } \beta < 0$$
(5)

In order to analyze the pressure dependence of the BE of A and B excitons, a precise knowledge of μ_{\perp} , μ_{\parallel} , $\epsilon_{\perp}(0)$, and $\epsilon_{\parallel}(0)$ is required. Our DFT calculations reveal a pressure dependence of μ_{\perp} and μ_{\parallel} that depend on the bands involved in the excitonic transition (see Figs. 8(b) and 8(c) of Appendix B) whereas $\epsilon_{\perp}(0)$ and $\epsilon_{\parallel}(0)$ have been shown to increase, theoretically and experimentally, as pressure increases (see Appendix D).

Before evaluating the BE of the A and B excitons in the frame of the Gerlach-Pollmann model, a word should be said about their respective Z_{00} function. From our results, it appears that

the Z_{00} function varies between 1 and 1.25 for the A exciton in the pressure range comprised in this work, which indicates a moderately anisotropic behavior. However, the Z_{00} function evaluated for the B exciton gives imaginary numbers in the whole pressure range explored due to the rare combination of a valence band with a saddle point and a 2D conduction band at the K point [Fig. 2(a)]. This makes that the B exciton is better described by an extremely anisotropic exciton, basically 2D; then, although the case of a 2D exciton is not explicitly considered in the Gerlach-Pollmann model, it would correspond to the case of $Z_{00}(2D)=2$ for any estimate of BE_{1B} by using this model.

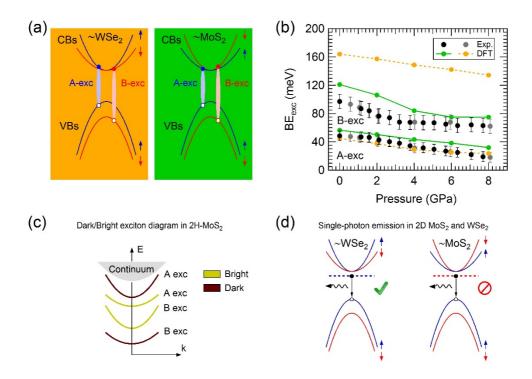


FIG. 3. (a) Schematic description of the two options of allowed A and B direct optical transitions, these following a WSe₂-like or a MoS₂-like spin-order configuration of a ML (b) Pressure dependence of the BE of ground A and B excitons of 2H-MoS₂, as extracted from the results shown in Fig. 1(b) by using that BE_{1A;B} = E_{0A;B} – E_{1A;B}. For each one of the optical transitions that may occur between the valence and conduction bands of 2H-MoS₂ and illustrated in (a), Error intervals have been propagated from data shown in Fig. 1(b). The pressure dependence of the BE of the related ground excitonic states has been calculated and included. The color-code used to plot the results of these calculations is the same as that used for the background of illustrations shown in (a), i.e., orange for WSe₂-like excitons and green for MoS₂-like excitons. (c) Proposed scheme of the bright and dark distribution of A and B excitons in 2H-MoS₂, as obtained from the results shown in (a). (d) Illustration of the difference radiative properties of eventual single photon emitters in 2D TMDs based on W and Mo transition metals, provided that spin-information of extended states remains unaltered when give rise to impurity-related localized states.

By introducing the pressure dependence of of μ_{\perp} , μ_{\parallel} , $\epsilon_{\perp}(0)$, and $\epsilon_{\parallel}(0)$ obtained by DFT calculations (see Appendix B and D) into Eqs. (4) and (5) and using a Z₀₀=2 for the B₁ exciton, we have calculated the pressure dependence of the BE1 of A and B excitons [Fig. 3(b)] for the WSe₂-like and MoS₂-like configurations [Fig. 3(a)]. By comparing these calculations with the experimental results, it appears that, although the pressure dependence of allowed optical transitions of the A exciton can be described by the two configurations illustrated in Fig. 3(a), these of the B-exciton can be only associated to that corresponding to the MoS2-like one. Therefore, since the possible options of spin-conserving excitonic transitions for the A and B excitons mutually exclude to each other, the MoS₂-like configuration shown in Fig. 3(a) appears to be the only one able to reproduce all experimental results described above. These results reveal that optical absorption measurements under pressure in 2H-MoS₂ here reported share with photoemission the ability to probe excitation processes localized within a particular single layer [26,27], with the advantage of reflecting the properties of the bulk material instead of these of the topmost layer. Our results evidence, although indirectly, that spin-polarized bands exist in centrosymmetric MoS₂ at the K point. Moreover, our results reveal that the hidden spin texture of valence and conduction bands of 2H-MoS₂ follows a spin order that agrees with that predicted in its ML at ambient pressure [12,21,22]. These results, also, shed some light on the origin of nontrivial circular polarization degree of the photoluminescence signal observed in bilayer transition-metal dichalcogenides under circularly polarized excitation light [3,59–62]

The results summarized in Fig. 3(b) naturally reveal also an unusual lift of the bright/dark degeneracy of A and B excitons in a centrosymmetric material (Figure 3(c)) that can be used as a platform for the study of the bright/dark nature of excitons in 2D materials [11–15]. From the results reported here, it appears that centrosymmetric MoS_2 varieties, such as the bilayer or bulk materials, are able to sustain bright and dark excitons (Fig 3(c)) with a larger splitting energy between dark and bright states than in its ML due to a larger difference between the μ_{\perp} of A and B excitons although the two lowest conduction bands are almost degenerate at the K point [14]. Also, these results can eventually provide for a route to clarify if single quantum emitters, ondemand emitters of one photon at a time into a given spatio-temporal mode [63], obey spin and valley optical selection rules of MLs of TMDs [Fig. 3(d)] [1–3]. An impurity or defect would be expected mainly to localize electronic states with larger spatial extension [64], i.e., electrons in

conduction band states with a lower effective mass [Fig. 3(d)]. In this context, optical recombination processes from these localized states were expected to occur with a higher probability in W-based TMDs than in Mo-based ones, provided that localized states conserved the spin-polarized nature of the unperturbed ones. More work should be required to elucidate this question. However, this may explain the lack of reports demonstrating the existence of single-photon emitters in MLs of Mo-based TMDs, [65] compared to these reported for the W-based ones [66–70].

The experimental results reported above and supported by our DFT calculations provide for strong evidences of an inherent spin-polarized nature of valence and conduction bands at the K point of 2H-MoS₂ at ambient pressure, which follows the spin-band sequence expected for 2D MoS₂. These evidences have been obtained by optical absorption and DFT techniques by using pressure as a variable to tune interlayer interactions, the curvature of mass of bands involved in optical transitions and the dielectric constant of 2H-MoS₂, without using spin-valley sensitive techniques such as circularly polarized light [1,3]. Then, we would like to stress that our measurements are not directly spin-sensitive. Keeping this in mind, it is worth noticing that our DFT calculations also predict that, as a consequence of subtle changes in the band structure induced by the increase of the interlayer interactions, not affecting the band dispersions, the material would be expected to experience an inversion of the spin-band sequence of its conduction bands, adopting a WSe₂-like configuration (Figure 3(a)) at high pressure. From our DFT calculations, such a spin-flip transition would be expected at pressures around 4 GPa. However, much work should be performed, by using circularly polarized light, for instance, to clarify the possible existence of a pressure-induced spin-flip transition in 2H-MoS₂ and its onset.

III. PRESSURE DEPENDENCE OF THE A AND B EXCITON BROADENING

The pressure dependence of the Γ_1 half width of the A_1 and B_1 discrete exciton lines of 2H-MoS₂ has been estimated (Fig. 4), by fitting Eq. (2) to the experimental data shown in Fig. 1(a). The Γ_1 half width of both excitons appear to exhibit a progressive and reversible broadening as pressure increases. At ambient pressure, values of 25.0 ± 0.5 and 40 ± 1 meV were found for Γ_{1A} and Γ_{1B} , respectively, which are in good concordance with reported values of the half-width

half maximum for the A_1 and B_1 exciton linewidths at 300 K [28,29,46]. The reversible broadening of the exciton linewidths observed with increasing pressure can be interpreted in terms of an increase of phonon-assisted scattering of electrons between the local conduction-band minimum at the K point and the absolute conduction-band minimum located at the Q point [37,38], i.e., at the midway along the Γ K high-symmetry direction. Such an increase of phonon-assisted scattering can be attributed to the relative downshift of the absolute conduction-band minimum observed [Fig. 2(a)] with respect to the local conduction-band minimum at the K point. In this way, A and B excitons, which are already resonant at ambient pressure, become more resonant as pressure increases. This pressure-induced broadening of the exciton lines, combined with the red shift of the high-energy absorption tail [the C feature identified in Fig. 1(a)] makes the B excitonic structure no longer observable for pressures above 8 GPa. The pressure dependence of Γ_{1A} and Γ_{1B} can be used to estimate the corresponding phonon deformation potential constant. Within the effective mass approximation, the exciton linewidth induced by phonon scattering can be expressed, as a function of the energy difference between the conduction band minima at the K and Q points (ΔE_{KQ}), as [37,38]:

$$\Gamma_{1A;B} = \Gamma_0 + \frac{N_Q m^*_Q^{3/2} D_{KQ}^2}{\sqrt{2} h \rho \Omega_Q} \left[\left(n(\Omega_Q) + 1 \right) \sqrt{\Delta E_{KQ} - \Omega_Q} + n(\Omega_Q) \sqrt{\Delta E_{KQ} + \Omega_Q} \right]$$
 Eq. (6)

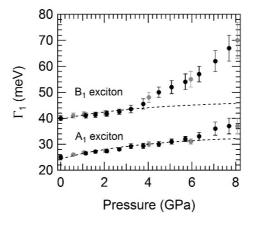


FIG. 4. Pressure dependence of the Γ_1 half-width of the first excitonic peaks (A₁ and B₁ excitons) of the fundamental absorption edge of 2H-MoS₂. Dashed lines are fitting curves obtained by means of Eq. (6). Although these curves have been plotted in the whole 0-8 GPa range, the fitting processes have been performed in the range of pressure comprised between 0 and 6 GPa (A₁ exciton) and 0-4 GPa (B₁ exciton), to conduct further discussion.

Where Γ_0 is a constant, h is the Planck's constant, ρ =5.06 g/cm^3 is the 2H-MoS₂ density, m^*Q is the density-of-states effective mass of the conduction-band minimum at the Q point, N_Q =6 is the number of equivalent indirect minima in the conduction band at the Q point, $n(\Omega_Q)$ and Ω_Q are the occupation number and energy of the phonons involved in the scattering, respectively, and D_{KQ} is the phonon deformation potential for intervalley phonon scattering. The pressure dependence of m^*Q and ΔE_{KQ} have been extracted from band structure calculations as these shown in Fig. 2(a). Recently, the nature of phonons responsible for intervalley scattering has been investigated in 2D MoS₂ and 2H-MoS₂ by means of double-resonance Raman spectroscopy and DFT calculations [71]. In that work, authors found that longitudinal acoustic phonons (these with Ω_Q =30 meV) dominate intervalley scattering in this material. By using these parameters, fitting Eq. (6) to the experimental data shown in Fig. 4, in the range of 0-6.5 and 0-4 GPa and for the A₁ and B₁ excitons, respectively, yields D_{KQ} =4.8 ± 0.2 eV/Å for the A₁ exciton, and D_{KQ} =4.3 ± 0.4 eV/Å for the B₁ exciton. These values appear to be in line with these found for diamond and zinc blende semiconductors [37,38].

These results evidence the strong role played by phonons-assisted scattering of electrons between the K and Q conduction band minima to determine the lifetime of both A and B excitons from ambient pressure to 4 GPa, which may be relevant for valleytronic applications of MoS_2 [1–5]. However, it can be noticed that the B_1 exciton exhibits a more pronounced broadening than the A_1 exciton as pressure increases from 4 GPa to 8 GPa (Fig. 4). This may be understood by the fact that the second lowest valence band at the Γ point upshifts in energy as pressure increases [Fig. 2(a)] and becomes resonant with states at the B valence band at the K point at 4 GPa. In consequence, an additional decay channel appears at 4 GPa for holes in the B valence band at the K point that is absent for holes at the A one, which enhances the pressure dependence of the Γ_1 of the B_1 exciton with respect to that of the A_1 exciton in the range of pressure comprised between 4 and 8 GPa. Only at pressures as high as ~7 GPa, additional decay channels appear accessible also for A excitonic transitions since, at these high pressures, the second lowest valence band at the Γ point becomes resonant with A valence-band states at the K point [Fig. 2(a)].

IV. PRESSURE DEPENDENCE OF THE INDIRECT BAND GAP OF 2H-MoS2

It has been theoretically predicted that MLs and bilayers of MoS2 can metallize under strain [72,73]. Similarly, a pressure-induced closure of the Eqind has been predicted to appear in bulk TMDs due to the consequent enhancement of the interlayer interactions [50-52,74]. In the particular case of bulk TMDs, the determination of the metallization onset is particularly relevant for the fundamental point of view due to the possibility that exotic insulator states, such as the socalled excitonic insulator [75], may exist just before the metallization onset [51,76]. Experimentally, a pressure-induced metallic state has been observed to develop in bulk in WSe₂ [74] and in MoS₂ [77-79]. However, some controversy seems to exist for the pressure values reported so far for the onset of metallization, at least for MoS2. On the one hand, electrical conductivity, X-ray diffraction, and Raman spectroscopy measurements performed in 2H-MoS₂, show that 2H-MoS₂ becomes metallic at pressures higher than 40 GPa [78], after completion of an isostructural phase transition that starts at 20 GPa [78]. On the other hand, similar studies [77] and impedance and Raman spectroscopy measurements carried out in 2H-MoS₂ [79] reveal that 2H-MoS₂ becomes metallic at pressures close to 20 GPa, after a structural lattice distortion [77,79]. Ab initio DFT calculations predict a pressure-driven metallization onset around 20 GPa [77], which arises from the overlap of the valence and conduction bands owing to sulphur-sulphur interactions as the interlayer spacing reduces. Recently, some authors have proposed that experimental conditions (in particular, the pressure medium used) [79] or excess sulfur content [80] can affect the properties of structural layered materials under pressure, which may drastically determine structural changes that seem to precede metallization of 2H-MoS₂ [77– 79].

In this section, we face the study the pressure dependence of the E_g^{ind} of 2H-MoS₂ and its eventual pressure-driven metallization onset, by means of optical absorption measurements under pressure. Results reported in the previous sections already envisage a progressive closure of the E_g^{ind} as pressure increases. In fact, the C-labelled feature [Fig. 1(a)] appears to redshift as pressure increases with no remarkable changes in shape. This feature has been attributed to

direct transitions involving valence band states located in the proximity of the Q point, where both valence and conduction bands have a minimum and the parallel shape of the bands causes a maximum in the joint density of states [31,32]. This assignment of the C-feature seems to be supported by our results. Figure 5 shows the pressure dependence of the E_{0C} related energy obtained by fitting Eq. (2) to the absorption coefficient spectra measured at different applied pressures [Fig. 1(a)]. In this figure, the pressure dependence of the band gap at Q point has been included, as obtained from DFT band-structure calculations as these shown in Fig. 2(a). Comparing the pressure coefficient of the C-feature (-9.3 \pm 0.9 meV/GPa) and that of the band gap at the Q point (-16 \pm 2 meV/GPa), it seems plausible that a progressive closure of the band gap of 2H-MoS₂ takes place as pressure increases [77–79].

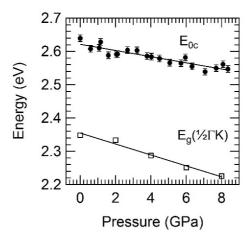


FIG. 5. Pressure dependence of high energy excitonic transitions giving rise to the C-labelled feature identified in the curves showed in Fig. 1(a). Error intervals have been obtained by fitting Eq. (2) to the experimental data in Fig. 1(a). The pressure dependence of the band gap at midpoint along the Γ K high-symmetry direction has been included, as obtained from DFT band-structure calculations [Fig. 2(a)].

In order to gain a deeper insight into the onset of the pressure dependence of the E_g^{ind} of 2H-MoS₂, we have performed optical transmittance measurements in bulk MoS₂ samples for pressures ranging from ambient conditions up to 26 GPa. An 11- μ m thick MoS₂ sample has been used for the measurements carried out between ambient conditions and 13.8 GPa, whereas for measurements between 15.7 and 26.1 GPa we have employed a thinner (1.2- μ m thick) MoS₂ sample. Figure 6(a) shows some examples of the absorption edge measured in MoS₂ samples at

hydrostatic pressures ranging from ambient pressure up to 26.1 GPa. As it can be observed in this figure, the indirect absorption edge of bulk MoS_2 shows a clear (and reversible) red shift with increasing pressure. The optical E_g^{ind} energy for all studied pressures has been determined from the linear fits of the square root of the low-energy tail of the absorption edge. Figure 6(b) shows the pressure-dependence of the optical E_g^{ind} resulting from these fittings. At room pressure, a value of E_g^{ind} =1.25 ± 0.04 eV has been found, which is in excellent agreement with that reported [54]. As shown in this figure, increasing hydrostatic pressure leads to a linear decrease of the optical E_g^{ind} from 1.26 eV at atmospheric pressure down to 0.33 eV at 26 GPa, with a pressure coefficient of -34.8±0.1 meV/GPa.

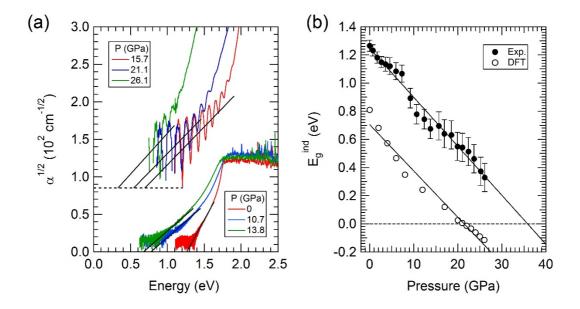


FIG. 6. (a) Square root of the absorption edge measured in 2H-MoS₂ samples 11- μ m thick (bottom spectra) and 1.2- μ m thick (top spectra) for pressures ranging from ambient conditions up to 26.1 GPa. Solid lines are linear fittings of $\alpha^{1/2}$ and extrapolated to α =0 to estimate the indirect band gap at each pressure. (b) Pressure dependence of the indirect band gap of 2H-MoS₂, as extracted from (a) (black circles) and as obtained by DFT calculations (white circles). Solid lines are linear fitting curves.

The results shown in Fig. 6 reflect a progressive closure of Eg^{ind} which indicate that, at pressures close to 26 GPa, 2H-MoS₂ still remains semiconducting in contrast to some experimental results reporting a semiconductor to metal transition of 2H-MoS₂ at pressures close to 20 GPa [77,79]. In order to estimate the metallization onset of 2H-MoS₂, it would be tentative

to extrapolate, towards higher pressures, the linear trend of Egind observed as pressure increases until 26 GPa. To test the validity range of this procedure, we have calculated the electronic band structure of 2H-MoS2 (Figure 7) at different pressures, by means of DFT in the local density approximation (LDA) [81]. As it can be observed in this figure, the uppermost valence band and the lowermost conduction band defining the indirect optical band gap of bulk MoS2 experience a progressive upshift and downshift, respectively, with increasing pressure, which allows us to obtain an estimate of the pressure coefficient of the Eqind. At this point, it must be outlined that DFT-LDA calculations are known to provide for accurate relative trends of band gaps as a function of pressure [49,77]. However, these methods provide for absolute band gap values that often differ from experimental ones in amounts that may vary from point to point of the reciprocal space and, consequently, give rise to inaccurate metallization-onset estimates [77]. To illustrate this, one can notice that our band structure calculations predict E_{0A}=1.613 eV, E_{0B}=1.835 eV, and Egind=0.805 eV at ambient pressure [Fig. 2(a)]. These values are in excellent agreement with DFT calculations performed under similar approaches (see, for instance, Table 2 in Ref. [49]). However, these calculations underestimate experimental direct band gap and Egind values by 0.30 eV [47] and 0.45 eV [54], respectively. Other DFT approaches can be used to obtain more accurate estimates of band gap values [49]. However, structures are hard to be relaxed under these approximations.

In Fig. 6(b), the pressure dependence of the Eg^{ind} of 2H-MoS₂, as calculated by DFT-LDA has been included. These calculations indicate that the Eg^{ind} linearly diminishes as the pressure increases, with a pressure coefficient of -32.9 meV/GPa that nicely agrees with that extracted from the experimental trend [Fig. 6(b)]. Then, apart from the band gap underestimation inherent to DFT-LDA calculations and discussed above, these results indicate that a semiconductor to metal transition in 2H-MoS₂ can be expected to occur at pressures higher than 26 GPa, with a metallization onset estimated around 35 GPa. These results seem to be in agreement with electrical conductivity, X-ray diffraction, and Raman spectroscopy measurements performed in 2H-MoS₂ [78], which show that 2H-MoS₂ remains semiconducting at 28 GPa and becomes metallic at pressures higher than 40 GPa.

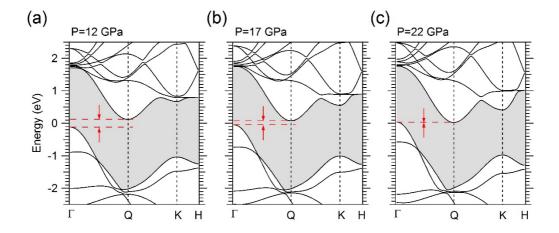


FIG. 7. Electronic band structure of 2H-MoS₂ calculated by DFT along the ΓK and the KH high-symmetry directions at 12 GPa (left), 17 GPa (center) and 24 GPa (rigth). Note the progressive closure of the indirect band gap as pressure increases, indicated by red dashed lines.

V. CONCLUSION

In summary, results here reported open the door for valleytronic and spintronic applications of not only MLs of MoS₂ but also its bilayers and trilayers. Centrosymmetric MoS₂ can sustain a non-expected lift of the degeneracy between bright and dark excitons that can be even stronger than in the single layer, due to the higher difference between the two conduction-band effective masses that predict band-structure calculations. Also, present results reported here shed some light on the origin of nontrivial circular polarization degree of the photoluminescence signal observed in bilayer transition-metal dichalcogenides under circularly polarized excitation light. Regarding the pressure dependence of the indirect band gap, the fact that 2H-MoS₂ can metallize at relatively accessible pressures opens the door for the search of exotic insulator states just before the onset of metallization, for which excitons located at midpoint along the ΓK high-symmetry direction may play a relevant role.

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APPENDIX A: METHODS

1. Optical characterization under pressure.

Thin MoS₂ samples with thicknesses varying from 0.13 to 11 µm were cleaved from large single crystals. Due to their weak interlayer bonding, face samples are perpendicular to the c axis. Samples were placed just after the cleavage along with several ruby chips in a 200-µm-diameter hole drilled on a 60-µm thick Inconel gasket and inserted between the diamonds of a diamondanvil cell of the membrane type [82]. For measurements in the ultra-violet, visible and nearinfrared range, a mixture of methanol, ethanol and water in the proportions 16:3:1 was used as hydrostatic pressure transmitting medium. For measurements in the mid-infrared, we used KBr as a transmitting medium. The pressure was determined through the ruby luminescence linear scale [83]. Room-temperature optical absorption of the samples was measured as a function of pressure using, for the ultra-violet and visible ranges, a deuterium lamp, spatial filters, reflective objectives, and a multichannel spectrophotometer. For the near-infrared, the light transmitted by the sample was focused on the entrance slit of a Jobin-Yvon M25 monochromator and collected by a Ge photodiode. All optical signals are synchronously measured by using a mechanical chopper and a lock-in amplifier. Optical transmittance measurements of bulk MoS2 under pressure in the mid-infrared were performed by means of Fourier transform infrared spectroscopy, by using an Interspectrum TEO-400 Michelson interferometer module and a non-commercial microsopic optical bench [84]. The obtained absorbance spectra were scaled to the theoretical values expected in the spectral range where the sample is transparent. The absorption coefficient (a) was calculated from the scaled absorbance and the sample thickness, which was obtained from the interference fringe pattern in the transparent region at room pressure. Its variation with

pressure was calculated from reported compressibility values [52]. The pressure dependence of the n_{\perp} has been obtained in the near- and mid-infrared. The n_{\perp} was measured from transmission interference fringe patterns at normal incidence by using the interference condition. The sample thickness and the interference order at ambient pressure were determined using reported values of the 2H-MoS₂ refractive index [85].

2. Density Functional Theory calculations.

Ab initio calculations were performed within DFT as implemented in the VASP code [86]. Core electrons were treated using the projector augmented wave method [87,88] and wave functions were expanded using a plane-wave basis set with an energy cutoff of 400 eV. For the exchange-correlation functional we used the Ceperley-Alder form of the LDA [81]. Relativistic effects were included by using a scalar relativistic Hamiltonian for both core and valence electrons and adding the spin-orbit coupling (SOC) term in the second-order approximation [89]. A 12x12x3 k-point grid was used to sample the Brillouin zone.

We used experimental a and c lattice parameters and, in order to consider the effects of pressure, we assumed that the 2H-MoS₂ unit cell evolves under compression as reported in Ref. [90]. Once the unit cell was fixed for each pressure the atomic coordinates were relaxed until forces were smaller than 0.01 eV/Å.

The static dielectric matrix was determined using density functional perturbation theory and including local field effects in the Hartree (RPA) approximation [91,92]. The frequency dependent dielectric matrix was determined by a summation over empty states as explained in Ref. [92]. Since we were only interested in a qualitative picture of the evolution of the frequency dependent dielectric matrix with pressure, its determination was done without taking into account local field effects and SOC.

APPENDIX B: PRESSURE DEPENDENCE OF CONDUCTION AND VALENCE BAND EFFECTIVE MASSES AT THE K POINT AND EXCITON MASSES

Figure 8(a) shows the pressure dependence of the effective mass of each one of the conduction and valence bands of 2H-MoS₂ along the Γ K (m*_{\perp}) and KH (m*_{\parallel}) high-symmetry directions (see inset of Fig 8(a) for the notation used to label each band). These effective masses

have been obtained by parabolic fitting of the **k**-dispersion of each band, as obtained by DFT calculations (as these shown in Fig. 2(a) for 0, 4 and 8 GPa). For convenience, we have adopted the criterion of assigning negative effective-mass values to convex bands. With regards to the valence bands, these results reveal that only their m^*_{\parallel} experience a notable dependence with pressure. With regards to the two lowest conduction bands at the K point, the most remarkable fact is the different trend with pressure obtained for their respective m^*_{\perp} around the K point.

From these results, the pressure dependence of the parallel (μ_I) and perpendicular (μ_L) to the c-axis exciton reduced mass has been calculated μ =(1/m* $_e$ -1/m* $_h$)-1 for each one of the optical transitions that may eventually occur between the as A valence band and the C1 and C2 conduction bands [Fig. 8(b)] and between the B valence band and the C1 and C2 conduction bands [Fig. 8(c)].

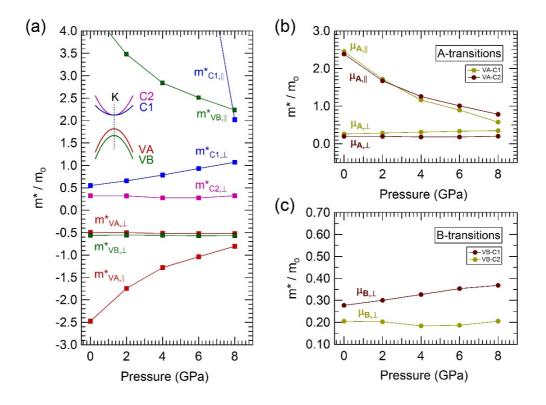


FIG. 8. (a) Pressure dependence of the effective mass of each one (see inset) of the two valence (VA and VB) and conduction bands (C1 and C2) of 2H-MoS $_2$ in the vicinity of the K point, as obtained by parabolic fitting of their respective band dispersion obtained by DFT along the Γ K (m^*_{\perp}) and KH (m^*_{\parallel}) high-symmetry directions. The m^*_{\parallel} of the C2 conduction band is not shown since it exceeds, by more than one order of magnitude, the scale range comprised by this plot, for pressures lower than 8 GPa. (b) and (c) Pressure dependence of the exciton reduced mass expected for each one of the

optical transitions that may occur between the A and B valence bands and the C1 and C2 conduction bands, respectively. For the B-transitions, μ_{BI} values are much higher than these of μ_{BL} , justifying their 2D nature.

APPENDIX C: SPIN AND BAND LOCALIZATION WITHIN EACH LAYER AS CALCULATED BY DFT

Electronic band structure calculations shown in Fig. 2(a), as well as these depicted in Fig. 9(a), suggest that conduction band states defining the direct band gap at the K point are strongly localized, whereas these of the two higher valence band exhibit a moderate localization degree. In order to explore the localization of the bands around the K-point, which plays a key role for optical absorption techniques to be able to probe intralayer optical transitions in 2H-MoS₂, we have defined the layer localization (LL) parameter

$$LL = \frac{|P(Mo_1) - P(Mo_2)|}{|P(Mo_1) + P(Mo_2)|}$$
, Eq. (C1)

where P(Mo_i) is the projection of the states of a particular band on the Mo atoms of the *i*-layer. In this way, states with LL=1 are completely confined within a particular layer whereas these with LL=0 are equally extended between two adjacent layers. Figure 9(b) shows the results of these calculations, which clearly reflect that conduction band states (these of the C1 and C2 bands) are strongly localized within a particular ML at the K point. Conversely, states at the VA and VB valence bands exhibit a moderate localization within a ML at the K point.

Figure 9(c) shows the component of the spin along the z-direction (m_z) for states coming from Mo atoms in one of the two MLs of the 2H-MoS₂ unit cell, for each valence and conduction band. For Mo atoms in the other ML of 2H-MoS₂, spin-projection values have an opposite sign. These calculations already reflect the spin band sequence expected for MLs of MoS₂ [See Fig. 3(a)] [12,48,93]. However, in order to evidence the existence of spin-layer polarization, m_z should be different from zero and LL should be close to the unity. Therefore, a spin-layer polarization parameter (SLP) defined as $SLP = m_z * LL$ can be used to quantitatively evaluate the degree of spin-layer polarization of states. Figure 9(d) shows the momentum dependence of the SLP parameter in the vicinity of the K point, which indicates that states involved in direct optical transitions at the K point exhibit a strong spin-layer polarized character, especially these of the conduction bands.

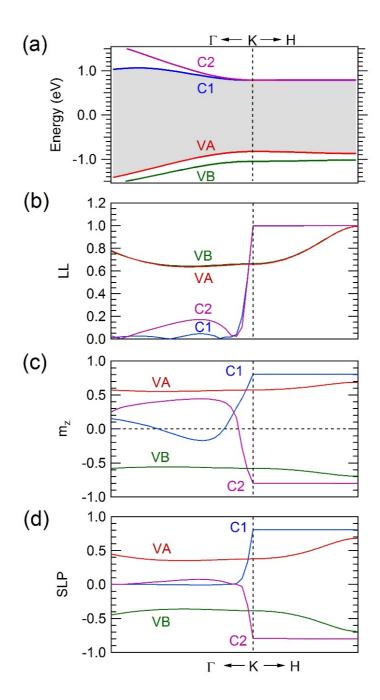


FIG. 9. (a) Dispersion of the valence and conduction bands of 2H-MoS $_2$ in the vicinity of the K point along the Γ K and KH high symmetry directions, as calculated by DFT. Grey shaded area represents the band gap. (b) Localization degree of states of the each one of the bands shown in (a) within a ML of 2H-MoS $_2$, as obtained by DFT calculations performed along the Γ KH directions. (c) Spin projection in the z direction (i.e., perpendicular to the layers) calculated for conductionand valence-band states located along the Γ KH directions. This spin projection has been calculated for one of the two MLs of the unit cell of 2H-MoS $_2$. (d) Momentum dependence, along the Γ KH directions, of the spin-layer polarization within a particular ML of 2H-MoS $_2$, as obtained by DFT. In all plots, bands have been labeled as in the inset of Fig. 8(a). Vertical dashed lines indicate the position of the K point.

APPENDIX D: PRESSURE DEPENDENCE OF THE STATIC DIELECTRIC CONSTANT

The dielectric function $\epsilon(\omega)$ = Re $\epsilon(\omega)$ + i Im $\epsilon(\omega)$ of 2H-MoS₂ has been calculated by DFT theory in the independent particle approximation. The results of these calculations are shown in Figure 10 under ambient pressure and under pressures of 4 and 8 GPa. From these calculations, it can be observed that, by increasing pressure, the low energy side of the Im $\epsilon(\omega)$ tends to shift to lower energies, with a more pronounced effect in the Im $\epsilon(\omega)$ evaluated in the direction parallel to the c-axis (Im $\epsilon_{II}(\omega)$). This effect is consistent with the progressive band-gap closure predicted by DFT (see Section IV) and also indicates that the Re $\epsilon(\omega)$, especially at low energies, increases as pressure does. This observation is relevant for a correct interpretation of the pressure dependence of the exciton absorption coefficient and exciton binding energies. Consequently, an accurate determination of the electronic contribution to the static dielectric constant ($\epsilon(0)$) is required. Figure 11 shows the pressure dependence of $\epsilon(0)$ as calculated by DFT, for the perpendicular and parallel to the c-axis directions ($\epsilon_{I}(0)$) and $\epsilon_{I}(0)$, respectively). In these calculations, local field effects have been included, which reveal that both the $\epsilon_{II}(0)$ and $\epsilon_{I}(0)$ tend to increase as the pressure increases from ambient conditions to 17 GPa.

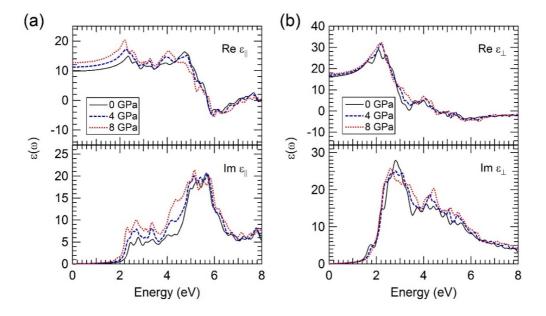


FIG. 10. Calculated real and imaginary parts of the dielectric function in the parallel (a) and perpendicular (b) to the c-axis directions, as obtained by DFT calculations in the independent particle approximation for bulk MoS₂ under ambient conditions and under pressures of 4 and 8 GPa.

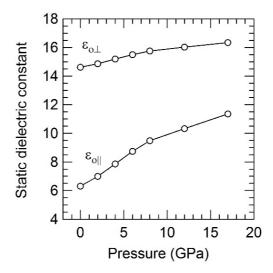


FIG. 11. Pressure dependence of $(\epsilon_{\perp}(0))$ and $\epsilon_{\parallel}(0)$, as obtained by DFT calculations in the local field approximation.

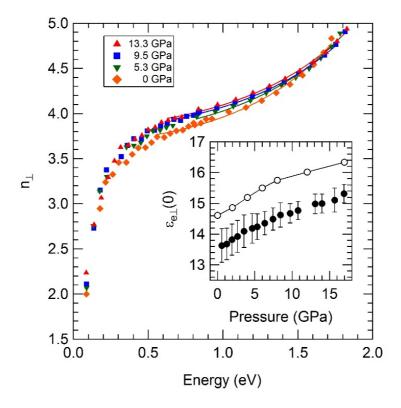


FIG. 12. Dispersion of the real part of the $n_{\perp}(\omega)$ of 2H-MoS₂ measured under different applied pressures. Solid lines are fitting curves to the experimental $n_{\perp}(\omega)$ dispersion curves as obtained by using Eq (S3). The inset shows the pressure dependence of $\epsilon_{\perp}(0)$ as obtained from these fittings. The pressure dependence of the $\epsilon_{\perp}(0)$ obtained by DFT has been also included in the inset, for comparison purposes.

In order to give experimental support to these calculations, we have determined the Re $\epsilon_{\perp}(\omega)$ of bulk MoS₂ in the mid-infrared (a 3.6-mm thick MoS₂ sample was employed) and near-infrared regions (a 1.2-mm thick MoS₂ sample was employed). The absorbance spectra acquired (not shown here) show a Fabry-Pérot interferometry pattern in which the appearance of maxima allows for the determination of the real part of the ordinary refractive index ($n_{\perp}(\omega)$) for each pressure applied, as they have been shown in Fig. 12. Each one of these $n_{\perp}(\omega)$ curves shows two asymptotic behavior at both sides of the energy range studied. The low-energy asymptotic behavior can be attributable to a resonance coming from the interaction of light with TO phonons, whereas the high-energy one corresponds to the electronic transitions which can be modelled by using an effective transition-gap called the Penn gap (E_{gP}) [94]. Focusing ourselves on the electronic contribution to $n_{\perp}(\omega)$, its energy dependence can be described by

$$n_{\perp}^{2}(\omega) = 1 + \left(\varepsilon_{\perp}(0) - 1\right) \left(\frac{E_{gP}^{2}}{E_{gP}^{2} - \omega^{2}}\right).$$
 Eq. (D1)

Therefore, by fitting Eq. (D1) to the dispersion $n_{\perp}(\omega)$ curves shown in Fig. 12, $\epsilon_{\perp}(0)$ can be estimated. The inset of Fig. 12 shows the pressure dependence of $\epsilon_{\perp}(0)$) as obtained by these fitting procedures. For comparison purposes, we have included the pressure dependence of $\epsilon_{\perp}(0)$ as obtained by DFT calculations to evidence that these calculations nicely reproduce the pressure dependence of $\epsilon_{\perp}(0)$ obtained experimentally, with a maximum 6% deviation.

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