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3 **Enhancing the Thermoelectric and Mechanical Properties of P-type PbS through**  
4 **Band Convergence and Microstructure Regulation**  
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3 **ABSTRACT:** Lead sulfide (PbS) shows notable thermoelectric properties as well as a  
4 relatively stable lattice structure. Nonetheless, the production cost of PbS materials  
5 remains relatively high, and its mechanical hardness is low, thus constraining its  
6 widespread application and commercial viability. In this study, we demonstrate a  
7 straightforward, cost-effective synthesis method at ambient temperature to produce PbS  
8 nanocrystals. By introducing controlled amounts of silver doping, we achieve p-type  
9 conductivity and fine-tune both the energy band structure and lattice configuration.  
10 Density functional theory (DFT) calculations show the introduction of silver shifts the  
11 Fermi surface into the valence band, facilitating band convergence and thereby  
12 enhancing the power factor. Besides, excess silver is present in the secondary phase of  
13 silver sulfide, which effectively diminishes the interface barrier and thereby enhances  
14 the Seebeck coefficient. The defects caused by doping, along with the dislocations and  
15 multiple interfaces introduced by secondary phases, effectively scatter phonons,  
16 reducing thermal conductivity to an ultra-low value of  $0.49 \text{ W m}^{-1}\text{K}^{-1}$  at 690 K.  
17 Moreover, the alterations in crystal structure and chemical composition within the  
18 composite contribute to improving its mechanical properties. Overall, optimized  
19 materials reach dimensionless thermoelectric figures of merit ( $ZT$ ) approximately ten  
20 times higher than pristine PbS at 690 K, alongside boasting a remarkable average  
21 hardness of 1.08 GPa at room temperature.  
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40 **KEYWORDS:** lead sulfide, energy band regulation, structural engineering, lattice  
41 thermal conductivity, mechanical hardness.  
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3 Thermoelectric materials enable the direct energy conversion between heat and  
4 electrical by exploiting the motion of charge carriers within solids. They hold  
5 significant promise for applications in green energy, space exploration, and solid-state  
6 refrigeration technologies. The efficiency of a thermoelectric device hinges on the  
7 resulting temperature gradient and three closely linked physical parameters:  
8 conductivity ( $\sigma$ ), Seebeck coefficient ( $S$ ), and thermal conductivity ( $\kappa$ ). These  
9 parameters combine into a dimensionless figure of merit for thermoelectric  
10 performance, denoted as  $ZT$ , and calculated by the formula:  $ZT = \sigma S^2 T / \kappa$ . Consequently,  
11 achieving high-performance thermoelectric materials necessitates traits such as  
12 elevated conductivity, significant Seebeck coefficient, and minimal thermal  
13 conductivity.

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23 Optimizing the electrical performance and Seebeck coefficient requires balancing  
24 the relationship between carrier concentration ( $n$ ,  $p$ ), carrier mobility ( $\mu$ ) and effective  
25 mass ( $m^*$ ). To maximize the power factor ( $PF$ ) of intrinsic semiconductor materials,  
26 doping becomes imperative for optimizing carrier concentration and electronic band  
27 structure<sup>1-7</sup>. For instance,  $p$ -type SnSe undergoes doping to modulate its energy band  
28 structure<sup>8-10</sup>, resulting in an increased  $n$  of approximately  $\sim 10^{19} \text{ cm}^{-3}$ , thereby  
29 significantly enhancing its  $\sigma$ . Conversely, semiconductors with inherently high carrier  
30 concentration, like SnTe and  $\text{Cu}_{2-x}\text{S}$ , require alterations in the lattice structure through  
31 doping<sup>11</sup> or the incorporation of a second phase<sup>12</sup> to mitigate  $n$ . Through mechanisms  
32 such as state density resonance<sup>13</sup>, energy band degeneracy<sup>14</sup>, and energy band  
33 convergence<sup>15</sup>, thermoelectric materials with low  $m^*$  can achieve significant  
34 enhancements in both  $m^*$  and  $S$ .

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45 Thermal conductivity is influenced by carrier thermal conductivity ( $\kappa_{ele}$ ), lattice  
46 thermal conductivity ( $\kappa_L$ ), and bipolar diffusion thermal conductivity ( $\kappa_b$ ).  $\kappa_L$  can be  
47 diminished by constraining phonon modes across all wavelength segments through  
48 multi-scale layered architecture designs<sup>16-20</sup>. Techniques including point defect  
49 scattering, dislocation scattering, grain boundary scattering, resonance scattering, and  
50 electroacoustic scattering are employed for this purpose.

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3 Overall, optimizing the composition, tuning defects, refining lattice structure, and  
4 engineering energy bands are effective strategies for enhancing the  $ZT$  value of  
5 semiconductor thermoelectric materials. These approaches facilitate coordinated  
6 control over  $n$ ,  $\mu$ , and  $\kappa_L$ , thereby improving overall performance.  
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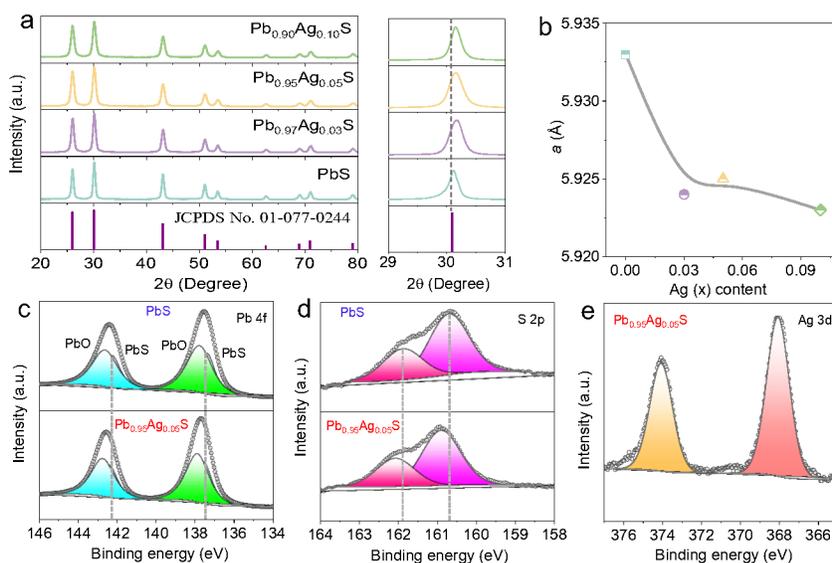
10 PbX (X=Te, Se, S) is a typical medium-temperature thermoelectric material and  
11 has been widely studied due to its superior thermoelectric properties. Among Pb  
12 chalcogenides, PbS is based on particularly abundant natural resources that makes it  
13 potentially cost-effective in numerous commercial applications<sup>21</sup>. However, PbS has  
14 relatively high  $\kappa_L$  and modest  $PF$ , which can be improved through doping and interface  
15 engineering. Doping can effectively adjust the electronic structure and energy band  
16 characteristics<sup>22–27</sup>, control the  $n$  and  $S$ , and thereby improve the  $PF$ . Besides, interface  
17 engineering can effectively scatter multi-scale phonons and reduce  $\kappa_L$ . Additionally,  
18 PbS exhibits poor mechanical hardness, which poses challenges to both its preparation  
19 and practical applications, particularly in the context of device miniaturization.  
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29 Here, we present a straightforward approach for synthesizing PbS nanocrystals,  
30 coupled with a novel method to tailor the position of the Fermi level through silver  
31 doping, thereby imparting  $p$ -type semiconductor characteristics. By fine-tuning the  
32 silver content, the energy band convergence is promoted, leading to a boost in the  $m^*$ ,  
33 consequently optimizing the  $PF$ . Additionally, the presence of silver introduces defects  
34 and increases the density of grain boundaries, which effectively scatter phonons,  
35 thereby reducing  $\kappa_L$ . Moreover, the defects and secondary phases induced by Ag doping  
36 generate additional dislocations and blocking points within the material. These features  
37 serve to impede atomic movement within the crystal lattice, consequently enhancing  
38 the material's hardness.  
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47 PbS nanocrystals were prepared by the reaction of  $\text{Pb}(\text{CH}_3\text{COO})_2 \cdot 3\text{H}_2\text{O}$  and  
48  $(\text{NH}_4)_2\text{S}$  at ambient temperature and conditions within an aqueous solvent (**Figure S1**).  
49 Further details regarding the synthesis procedure can be found in the Supplementary  
50 Information (SI). The reaction yields nanocrystals with an average size of  
51 approximately 17 nm (**Figure S2**). XRD analysis revealed the particles to exhibit a  
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3 distinctly crystalline cubic PbS structure, as shown in **Figure S2c**. High-resolution  
4 transmission electron microscopy (HRTEM) analysis of the crystal displayed in **Figure**  
5 **S2d** show the PbS lattice fringes to be 0.344 nm, 0.330 nm, and 0.296 nm, at 70.39°  
6 and 120.78°. These values correspond to the cubic PbS phase, observed along its [1-10]  
7 zone axis.  
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12  $\text{Pb}_{1-x}\text{Ag}_x\text{S}$  ( $x=0, 0.03, 0.05, \text{ and } 0.10$ ) nanoparticles were produced by the reaction  
13 of proper amounts of  $\text{Pb}(\text{CH}_3\text{COO})_2$  and  $\text{AgNO}_3$  with  $(\text{NH}_4)_2\text{S}$  in water and at ambient  
14 temperature, pressure and atmosphere. The XRD pattern of the  $\text{Pb}_{1-x}\text{Ag}_x\text{S}$  nanopowders  
15 revealed the presence of the cubic PbS phase, with no discernible peaks indicating the  
16 presence of additional Ag or  $\text{Ag}_x\text{S}$  phases, which could be attributed to the low content  
17 of silver. The XRD diffraction peaks of the Ag-doped samples shift towards higher  
18 angles, indicating that  $\text{Ag}^+$ , with a smaller ionic radius, partially replace  $\text{Pb}^{2+}$ , within  
19 the PbS lattice, which results in a reduction in the lattice parameters. However, with  
20 increasing silver content, the diffraction peak shift reaches a plateau, suggesting that  
21 the solubility of silver has reached saturation (**Figure 1a and 1b**). Within the  
22 experimental error of the technique, SEM-EDX analysis revealed a strong correlation  
23 between the observed amount of silver within the material and the nominal amount  
24 introduced (**Figure S3 and Table S1**). Thus, at high Ag loadings, the excess silver must  
25 exist within the material in the form of secondary phase.  
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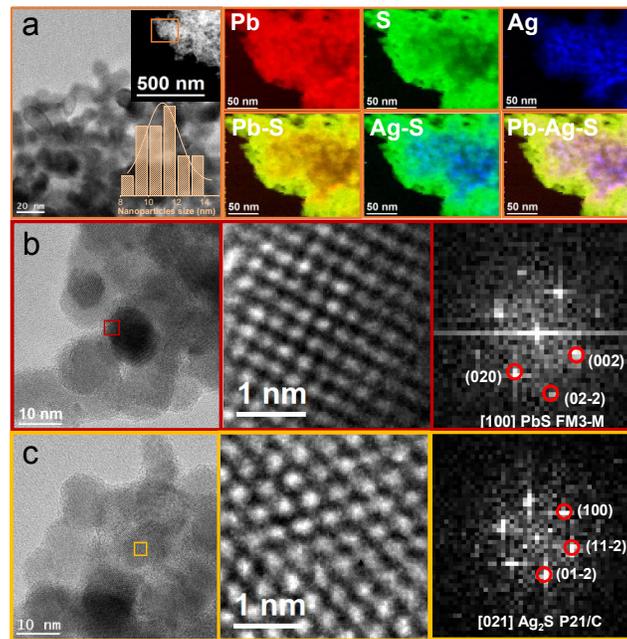


**Figure 1.** a) XRD patterns of the  $\text{Pb}_{1-x}\text{Ag}_x\text{S}$  nanoparticles, and magnification of the (200) XRD peak. b) Experimental lattice parameters calculated from XRD patterns. c-e) High resolution Pb 4f (c), S 2p (d) and Ag 3d (e) XPS spectra of  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$ .

The high-resolution XPS spectra of PbS and  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$  nanoparticles are shown in **Figure 1c-e**. The bands observed at 142.2 and 137.4 eV correspond to the Pb 4f<sub>5/2</sub> and Pb 4f<sub>7/2</sub> core levels, of  $\text{Pb}^{2+}$  cations within the PbS chemical environment<sup>24</sup>. The bands at 142.6 and 137.8 eV are attributed to the Pb 4f core levels of  $\text{Pb}^{2+}$  within a PbO chemical environment<sup>24</sup>. The PbO presence indicates partial surface oxidation of the material upon exposure to the ambient atmosphere. In the  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$  sample, the peak positions of  $\text{Pb}^{2+}$  shift to 142.4 and 137.6 eV, respectively. The S 2p XPS spectrum of PbS exhibits two peaks at 161.8 and 160.7 eV, corresponding to the S 2p<sub>1/2</sub> and S 2p<sub>3/2</sub> core levels of  $\text{S}^{2-}$  within the PbS structure<sup>28</sup>. For the  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$  sample, the peak positions of  $\text{S}^{2-}$  are also blue-shifted in the same magnitude as the Pb ions, up to 162.0 and 160.9 eV, respectively. The XPS spectra blueshifts obtained with the Ag introduction are associated with the presence of Ag ions with a slightly higher electronegativity than Pb within the lattice and to the related lattice contraction<sup>29-31</sup>. The Ag 3d XPS spectrum of  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$  exhibited two peaks at 374.1 and 368.0 eV, representing the Ag 3d<sub>3/2</sub> and Ag 3d<sub>5/2</sub> core levels of  $\text{Ag}^+$  within  $\text{Ag}_2\text{S}$ <sup>32</sup>.

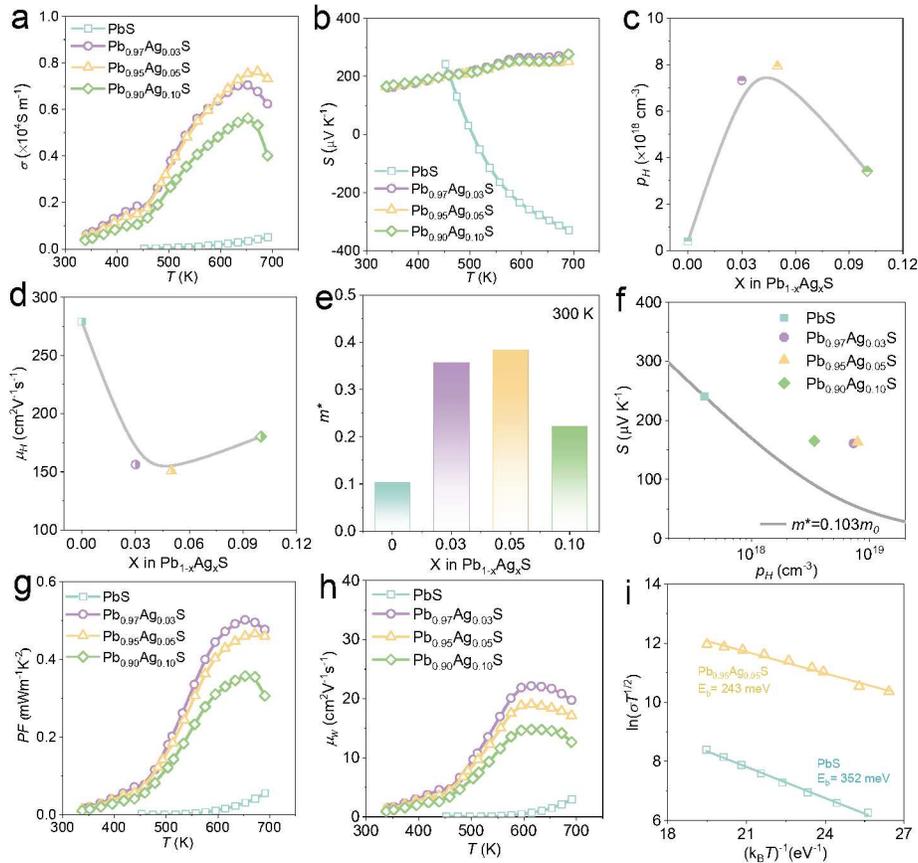
**Figure 2** shows the representative HRTEM micrographs and the electron energy loss spectroscopy (EELS) elemental composition maps of the  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$  nanoparticles. We observe the presence of Ag to result in a significant particle size reduction, with the average particles size of the  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$  nanoparticles around 12 nm. EELS compositional maps reveal that Pb and S are uniformly distributed within the nanoparticles, but the distribution of Ag appears to be less uniform. **Figure 2b** shows an HRTEM micrograph of a PbS particle within the  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$  sample. For this particle, the PbS lattice fringe distances were measured at 0.289 nm, 0.210 nm and 0.304 nm, at 44.58° and 87.91° which could be interpreted as the cubic PbS phase, visualized along its [100] zone axis. **Figure 2c** displays an HRTEM micrograph taken

from the  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$  sample, revealing the presence of the  $\text{Ag}_2\text{S}$  monoclinic phase (space group = P21/C). Examination of the  $\text{Ag}_2\text{S}$  lattice fringes yielded measurements of 0.337 nm, 0.340 nm, and 0.348 nm, at angles of  $56.48^\circ$  and  $117.18^\circ$ . These parameters are consistent with the monoclinic  $\text{Ag}_2\text{S}$  phase with lattice parameters  $a=4.2310 \text{ \AA}$ ,  $b=6.9300 \text{ \AA}$ , and  $c=9.5260 \text{ \AA}$  visualized along its [021] zone axis.



**Figure 2.** a) Representative TEM micrographs of  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$  nanoparticles and histogram of the particle size distribution (inset), EELS chemical composition maps. b,c) HRTEM micrographs of a  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$  sample, and their corresponding electron diffraction patterns.

**Figure 3** shows the measured  $\sigma$ ,  $S$  and Hall effect of the  $\text{Pb}_{1-x}\text{Ag}_x\text{S}$  pellets. The  $\sigma$  of the pure PbS sample is inherently low, rendering it impractical for measuring at room temperature. This conductivity escalates with temperature as it corresponds to an intrinsic or moderately doped semiconductor (**Figure 3a**). With Ag doping, the  $\sigma$  experiences a notable surge, but maintains its dependence with temperature below 650 K, where  $\sigma$  peaks before gradually declining. The rise in  $\sigma$  with Ag doping primarily stems from the increase of hole concentration ( $p$ ). In addition, the decline in conductivity beyond 650 K predominantly arises from the gradual decrease of mobility experience by the high density of thermally excited bipolar carriers at this temperature.



**Figure 3.** a-h) Thermoelectric properties of  $\text{Pb}_{1-x}\text{Ag}_x\text{S}$  pellets. a) Temperature dependence of electric conductivity. b) Temperature dependence of Seebeck coefficient ( $S$ ). c) Ambient temperature Hall carrier concentration ( $p_H$ ), d) carrier mobility ( $\mu_H$ ) and e) effective mass ( $m^*$ ). f) Pisarenko plot. g) Power factors ( $PF$ ). h) Temperature dependence of weighted mobility ( $\mu_W$ ). i) Energy barrier scattering in  $\text{PbS}$  and  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$  pellets.

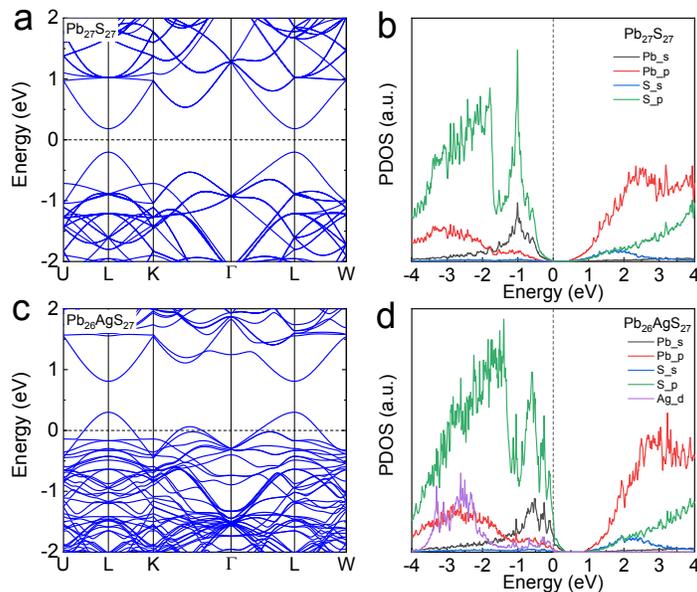
$\text{PbS}$  exhibits a positive Seebeck coefficient at temperatures below 500 K and becomes negative  $S$  at higher temperature (**Figure 3b**). The p-type semiconductor characteristic at low temperatures is primarily attributed to the presence of  $\text{PbO}$  on the surface of the nanoparticles grown during the synthesis process or the posterior exposition of the particles to air, and which inherently exhibits p-type semiconductor properties. As temperature rises, the concentration of thermally generated charge carriers gradually surpasses the density of holes associated with the presence of  $\text{PbO}$  and the intrinsic n-type characteristics of  $\text{PbS}$  become predominant. In contrast, all the

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3 Ag-doped samples consistently display a p-type semiconductor characteristic across the  
4 entire temperature range. This variation primarily stems from the substitution of  $\text{Pb}^{2+}$   
5 with  $\text{Ag}^+$ , which leads to an increase in hole concentration.  
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9 Hall measurements at room temperature were conducted to determine the Hall hole  
10 concentration ( $p_H$ ) and mobility ( $\mu_H$ ) as shown in **Figure 3c** and **3d**. The  $p_H$  of PbS is  
11  $4.0 \times 10^{17} \text{ cm}^{-3}$  and increases significantly when doped with a low content of Ag. The  $p_H$   
12 of  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$  is  $7.9 \times 10^{18} \text{ cm}^{-3}$ , about one order of magnitude higher than PbS, which  
13 is associated with the acceptor role played by  $\text{Ag}^+$  ions at the  $\text{Pb}^+$  sites within the PbS  
14 lattice. The  $p_H$  decreased in samples with high Ag content, possibly due to an increase  
15 in the nucleated  $\text{Ag}_2\text{S}$  domains. As anticipated,  $\mu_H$  decreases with Ag doping, which is  
16 related to the increase of atomic scattering centers and the distorted lattice.  
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23 Effective mass ( $m^*$ ) values were estimated using a single parabolic band (SPB)  
24 model, thereby encompassing the overall contribution from multiple valence bands in  
25 the estimation. **Figure 3e** illustrates that Ag doping leads to an increase in the  $m^*$  since  
26 the downward of Fermi level to valence band. **Figure 3f** displays the Pisarenko plot  
27 including the  $S$  and  $p_H$  of all the samples at room temperature. The  $S$  of the samples  
28 containing Ag are slightly above the theoretical curve plotted considering the  $m^*$  of  
29 PbS. This result is consistent with the electronic band structure calculations below.  
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36 The  $\sigma$  and  $S$  values of  $\text{Pb}_{1-x}\text{Ag}_x\text{S}$  were used to compute the power factors ( $PF =$   
37  $\sigma S^2$ ) as depicted in **Figure 3g**. The  $PF$ s of the Ag-doped samples were significantly  
38 higher than those of PbS, and they demonstrated a significant enhancement with rising  
39 temperature up to 650 K. Above 650 K, the  $PF$ s of the Ag-doped samples experienced  
40 a slight decrease, associated with the decreased electrical conductivity. The highest  $PF$   
41 value reached  $0.51 \text{ mWm}^{-1}\text{K}^{-2}$  at 650 K, obtained from the  $\text{Pb}_{0.97}\text{Ag}_{0.03}\text{S}$  sample. This  
42 value is much higher than that of PbS, which displayed a maximum  $PF$  value of  $0.03$   
43  $\text{mWm}^{-1}\text{K}^{-2}$  at 650 K.  
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**Figure 4.** (a, c) Calculated electronic band structure and (b, d) density of states for PbS and Ag-doped PbS, respectively. The dashed line refers to Fermi level.

To explore the influence of Ag doping on the electronic band structure of PbS, we conducted density functional theory (DFT) calculations. **Figure 4** shows the calculated electronic band structure and density of states (DOS) of PbS and Ag-doped PbS. The electronic band structure illustrates that upon the substitution of Pb with Ag, the Fermi level shifts into the valence band, thereby attaining p-type semiconductor characteristics. Additionally, the introduction of Ag doping resulted in an augmentation of the band gap of PbS from 0.38 eV to 0.48 eV. Furthermore, there's a reduction in the energy difference between L and  $\Sigma$  valleys, indicating a tendency towards energy band convergence, which is poised to enhance the power factor. Following Ag doping, a substantial increase is observed in the DOS slope at the Fermi level, thereby aiding in the enhancement of the  $m^*$  and Seebeck coefficient.

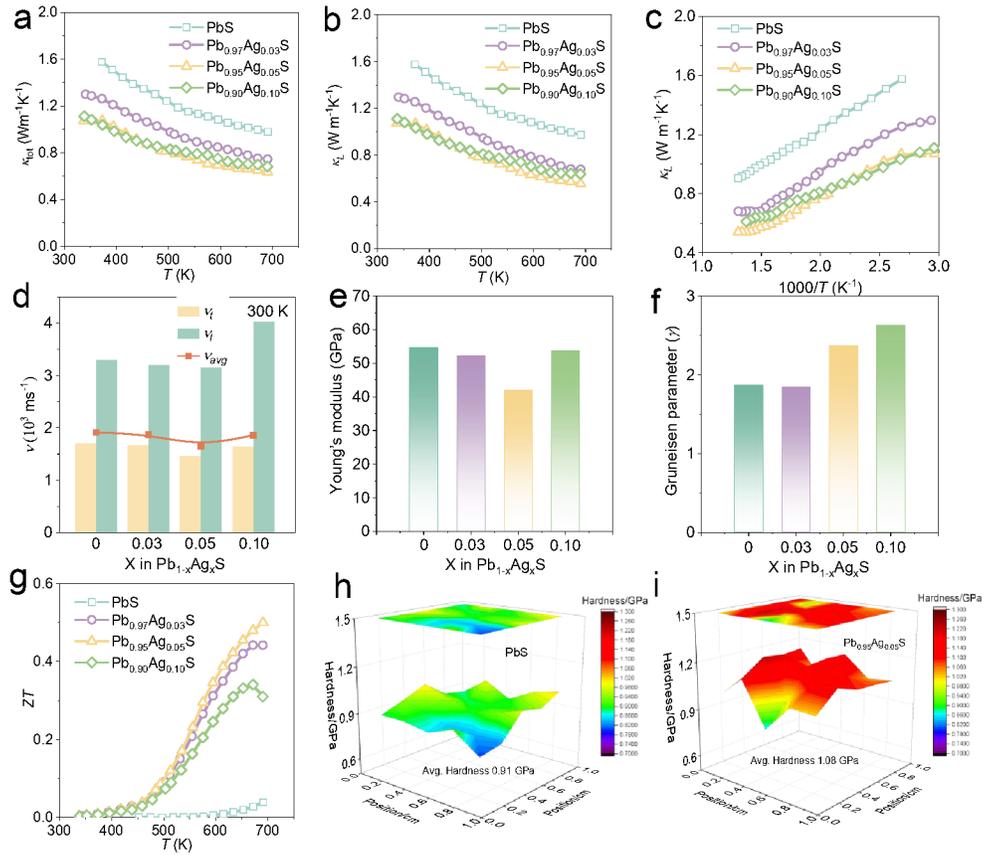
The weighted mobility ( $\mu_W$ ) was calculated using  $\sigma$  and  $S$  values, providing a mobility parameter unaffected by  $p_H$ . This calculation considers the average mobility across all conductive channels, thus offering a comprehensive assessment of the overall conductivity<sup>33</sup>. Detailed calculation formulas can be found in the SI.  $\mu_W$  increases with Ag doping (**Figure 3h**). The  $\text{Pb}_{0.97}\text{Ag}_{0.03}\text{S}$  sample exhibited the highest  $\mu_W$  value at 22.1

cm<sup>2</sup>V<sup>-1</sup>s<sup>-1</sup> at 613 K, which denotes superior electrical transport properties. The observed variations in mobility often suggest a hopping process or energy barrier scattering. Here, we consider a grain boundary barrier scattering mechanism to describe mobility, a model that has been extensively applied to thermoelectric materials. Assuming a uniformly distributed concentration of ionized carrier traps and barrier, and a grain boundary thickness that is much less than the crystallite size  $L$ , the effective mobility ( $\mu$ ) is given by<sup>34</sup>

$$\mu = Le \left( \frac{1}{2\pi m^* k_B T} \right)^{1/2} \exp \left( \frac{-E_B}{k_B T} \right) \quad (1)$$

where  $E_B$  is the energy barrier. A clearly linear relationship is seen between  $\ln(\mu T^{1/2})$  and  $(k_B T)^{-1}$  in **Figure 3i**, with a slope equal to  $E_B$ .  $E_B$  was decreased from 352 meV to 243 meV with Ag doping. This indicates that Ag doping reduces the grain boundary barrier and increases the effective mobility, which is consistent with the results in

**Figure 3h**.



**Figure 5.** a-c) Thermoelectric properties of  $\text{Pb}_{1-x}\text{Ag}_x\text{S}$  pellets. Temperature dependence of a)

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3 thermal conductivity ( $\kappa_{total}$ ) and b) lattice thermal conductivity ( $\kappa_L$ ). c) The plot of  $1000/T$ -dependent  
4  $\kappa_L$ . d) Sound velocity, e) Young's modulus ( $E$ ) and f) Grüneisen parameter ( $\gamma$ ) of  $Pb_{1-x}Ag_xS$  pellets  
5 at room temperature. g)  $ZT$  value. h-i) 3D cloud diagram of hardness for PbS and  $Pb_{0.95}Ag_{0.05}S$   
6 pellets. i) Average modulus and average hardness of PbS and  $Pb_{0.95}Ag_{0.05}S$  pellets.  
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12 The  $\kappa_{total}$  values of all the  $Pb_{1-x}Ag_xS$  ( $x = 0, 0.03, 0.05, 0.10$ ) samples are shown  
13 in **Figure 5a**. Ag doping significantly reduced the  $\kappa_{total}$ . We calculate  $\kappa_{ele}$  (**Figure S4**)  
14 and  $\kappa_L$  (**Figure 5b**) of all the samples by the Wiedemann-Franz law,  $\kappa_{ele} = L_o \sigma T$  and  
15  $\kappa_L = \kappa_{total} - \kappa_{ele}$ , where  $L_o$  is the Lorenz number  $\sim 1.7 \times 10^{-8} \text{ V}^2 \text{K}^{-2}$  obtained from the  
16 measured  $S$  values (**Figure S5**). **Figure 5b** shows that Ag doping significantly reduces  
17 the  $\kappa_L$  of the sample over the entire temperature range, especially for  $Pb_{0.95}Ag_{0.05}S$  that  
18 reaches  $0.48 \text{ W m}^{-1} \text{K}^{-1}$  at 690 K. This reduction in  $\kappa_L$ , is related to a multiscale phonon  
19 scattering phenomena that includes the introduced point defects, the lattice dislocation  
20 caused by Ag doping, and the multi-grain boundary introduced by the secondary phase.  
21 **Figure 5c** shows the plot of  $1000/T$ -dependent  $\kappa_L$  for all samples. Only the undoped  
22 sample shows a roughly linear relationship, indicating that the Umklapp phonon  
23 scattering plays a critical role in PbS<sup>22</sup>. Ag-doped samples display a notably restrained  
24 bipolar thermal conductivity in contrast to that of the pristine PbS at high temperature,  
25 which might be ascribed to the diminished bipolar diffusion owing to the increased  
26 band gap<sup>11</sup>.  
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40 In pursuit of a deeper comprehension of the mechanism underlying the achieved  
41 ultra-low  $\kappa_L$ , we conducted measurements of the sound velocity of the samples at room  
42 temperature. The  $\kappa_L$  is related to the average sound velocity ( $v_{avg}$ ), Grüneisen parameter  
43 ( $\gamma$ ), Young's modulus ( $E$ ), etc. This relationship is commonly described by the Debye-  
44 Callaway equation<sup>15</sup>:  
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$$\kappa_L = \frac{1}{3} C_v v_{avg} l \quad (2)$$

49 where  $C_v$  is the specific heat derived from the Dulong–Petit limit and  $l$  is the phonon  
50 mean free path. The  $v_{avg}$  is calculated from the longitudinal ( $v_l$ ) and shear velocity ( $v_t$ )<sup>6,20</sup>.  
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$$v_{\text{avg}} = \left[ \frac{1}{3} \left( \frac{1}{v_l^3} + \frac{2}{v_t^3} \right) \right]^{-1/3} \quad (3)$$

The  $v_l$  and  $v_t$  can be acquired directly in the ultrasonic pulse echo measurements, shown in **Figure 5d**. The  $v_{\text{avg}}$  decreases with Ag doping, and achieved a minimum value of  $1.6 \times 10^3 \text{ m s}^{-1}$  in  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$ . The decrease of sound velocity may be due to the weaker interatomic bonding between Ag and S.

According to the Debye model, there is a relationship between  $l$  and the phonon lifetime  $\tau$ :  $l = v_{\text{avg}}\tau$ . The  $\tau$  can be calculated using the Grüneisen parameter ( $\gamma$ ) and the Young's modulus ( $E$ ), typically approximated as<sup>35</sup>:

$$\tau = \frac{\hbar}{2k_B T \gamma E} \quad (4)$$

The  $E$  and  $\gamma$  can be calculated from the sound velocity, shown in **Figure 5e-f** and **Table S2**. Detailed calculation formulas can be found in the SI. The  $E$  decreases slightly with Ag doping, but  $\gamma$  increases significantly, from 1.87 in PbS to 2.37 in  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$ . Hence, the notably low  $\kappa_L$  of  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$ , attributed to its lower phonon transmission velocity and larger  $\gamma$ . In addition, shear modulus and Poisson ratio also can be calculated from the sound velocity<sup>20</sup>, which also related to the  $\kappa_L$  (**Table S2**).

Overall, the combination of enhanced electrical and degraded thermal transport properties resulted in a peak  $ZT$  value of 0.5 at 690 K for  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$ , significantly surpassing that of undoped PbS (**Figures 5g**). Moreover, the mechanical properties of the bulk samples were evaluated using nanoindentation, using the Nano-Blitz 3D method. Analysis of 3D hardness diagrams indicates a notable increase in hardness for the  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$  sample compared to the PbS sample, the average hardness increased from 0.91 GPa in PbS to 1.08 GPa in  $\text{Pb}_{0.95}\text{Ag}_{0.05}\text{S}$  (**Figure 5h-i**). The improvement in mechanical hardness is typically associated with alterations in the crystal structure and chemical composition of the material<sup>36</sup>. In the hot-press process, partial Ag replacement of Pb introduces point defects, lattice dislocation and the  $\text{Ag}_2\text{S}$  secondary phase. The introduction of this second phase can elevate the density of dislocations and barriers within the material, thereby hindering the movement and slipping of dislocations<sup>6,13</sup>. This increased structural complexity enhances the material's resistance to deformation and plasticity, ultimately improving its mechanical strength.

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3 In summary, we reported a straightforward aqueous synthesis method to produce  
4 Ag-doped PbS nanocrystals with high yield and scalability. The bulk composites were  
5 prepared by hot pressing, and the effect of Ag doping on the thermoelectric properties  
6 and mechanical hardness of PbS was discussed. DFT calculations revealed that the  
7 presence of Ag promoted band convergence and shifted the Fermi level towards the  
8 valence band, which resulted in p-type semiconductor characteristics. Furthermore,  
9 through structural analysis, we showed that a portion of Ag exists as a secondary phase  
10 of Ag<sub>2</sub>S, which increases the interfacial density within the sample, consequently  
11 enhancing phonon scattering and reducing lattice thermal conductivity. This alteration  
12 in microstructure by Ag doping also resulted in an enhancement of the mechanical  
13 hardness of the material. Overall, this study demonstrated an enhancement of the  
14 thermoelectric properties and mechanical hardness of PbS by optimizing both band  
15 structure and microstructure, which provides a solid experimental basis for the potential  
16 commercialization of systems based of this or related thermoelectric materials.  
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### 46 **Author Contributions**

47  
48 The manuscript was written through contributions of all authors. All authors have given  
49 approval to the final version of the manuscript.  
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### 54 **Notes**

The authors declare no competing financial interest.

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