**Mathematics and Big Data**  
2015/2016

**Contact**

Name: Mercè Farré Cervelló  
Email: Merce.Farre@uab.cat

**Teachers**

Jaume Aguadé Bover  
Joan Valls Marsal  
Carme Font Moragon

**Prerequisites**

Students should have basic knowledge of statistics, linear algebra and linear models and programming skills. A previous experience with statistical software “R” will be helpful.

**Objectives and Contextualisation**

The aim of the subject is to learn and apply various mathematical and statistical methods related to the discovery of relevant patterns in data sets. Nowadays, huge amounts of data are being generated in many fields, and the goal is to understand what the data say. This process is often called learning from data.

The first part of the course deals with the spectral and singular value decomposition of matrices from standpoints algebraic and geometric. These decompositions are the basis of the principal component analysis (PCA) and other factorial methods that could be applied to reduce the data dimension and visualize some patterns. A second part is devoted to classical clustering methods, a broad class of methods for discovering unknown subgroups in data. PCA and clustering are two particular types of unsupervised statistical learning. In a third step, we also focus in clustering methods but with a markedly different approach, using topology based methods to extract insights from the shape of complex data sets. The final part of the course will be devoted to supervised statistical learning: regression analysis, classification and regression trees and neural networks, among others.

**Skills**

- Analyse, synthesise, organise and plan projects in the field of study.
- Apply logical/mathematical thinking: the analytic process that involves moving from general principles to particular cases, and the synthetic process that derives a general rule from different examples.
• Apply techniques for solving mathematical models and their real implementation problems.
• Conceive and design efficient solutions, applying computational techniques in order to solve mathematical models of complex systems.
• Formulate, analyse and validate mathematical models of practical problems in different fields.
• Isolate the main difficulty in a complex problem from other, less important issues.
• Solve complex problems by applying the knowledge acquired to areas that are different to the original ones.

Learning outcomes

1. Analyse, synthesise, organise and plan projects in the field of study.
2. Apply Bayesian statistical techniques to predict the behaviour of certain phenomena.
3. Apply logical/mathematical thinking: the analytic process that involves moving from general principles to particular cases, and the synthetic process that derives a general rule from different examples.
4. Identify real phenomena as models of stochastic processes and extract new information from this to interpret reality.
5. Isolate the main difficulty in a complex problem from other, less important issues.
6. Solve complex problems by applying the knowledge acquired to areas that are different to the original ones.
7. Solve real data analysis problems by identifying them appropriately from the perspective of Bayesian statistics.
8. Use appropriate statistical packages and Bayesian methods solutions to solve specific problems.

Content

Introduction: Statistical learning, concept, methods, and examples

1. Matrix decompositions and factorial methods.
   1.1. Spectral decomposition.
   1.2. Singular value decomposition.
   1.3. Principal component analysis.
   1.4. Multidimensional scaling.
   1.5. Exploratory factor analysis.
   1.6. Correspondence analysis.

2. Classical clustering methods
   2.1. Hierarchical clustering.
   2.2. K-means Clustering.
   2.3. Model-based methods.

3. Introduction to Topological Data Analysis
   3.1. What is Topology and why it may be useful to data analysis.
   3.2. Simplicial complexes and homology.
   3.3. The Cech complex.
   3.4. Discretization and persistence.
   3.5. A classic example: Mumford’s photographs.
   3.6. Implementing topological data analysis.
   4.7. Visualization through stratification and clustering.

4. Supervised learning methods.
4.1. Introduction to statistical modelling.
4.2. Tree-based methods.
4.3. Neural networks.
4.4. Random forests.
4.6. BIG DATA in research: some examples in biomedicine.

Methodology

Lectures, supervised exercises and autonomous activities directed to realise a data analysis project based on statistical learning tools.

Activities

<table>
<thead>
<tr>
<th>Title</th>
<th>Hours</th>
<th>ECTS</th>
<th>Learning outcomes</th>
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<td>Type: Directed</td>
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<tr>
<td>Lectures</td>
<td>34</td>
<td>1.36</td>
<td>1, 4, 7</td>
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<tr>
<td>Type: Supervised</td>
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<tr>
<td>Completion of exercises</td>
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<td>1.44</td>
<td>2, 3, 7, 8</td>
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<tr>
<td>Type: Autonomous</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Personal study, readings</td>
<td>20</td>
<td>0.8</td>
<td>2, 4, 7</td>
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<tr>
<td>Project</td>
<td>48</td>
<td>1.92</td>
<td>1, 2, 3, 4, 5, 6, 7, 8</td>
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</table>

Evaluation

First, it is necessary to attend at least 80% of all sessions. In the evaluation, the following factors will be taken into account:

Exercises (40%): Completion and presentation of the proposed exercises.

Exams (20%): At the end of each block, a test in which the achievement of the objectives will be assessed is performed.

Project (40%) (in pairs): The work consists in finding a appropriate database, analyze the data using two or more techniques learned during the course and write a final report to be presented publicly.

Evaluation activities

<table>
<thead>
<tr>
<th>Title</th>
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<th>Hours</th>
<th>ECTS</th>
<th>Learning outcomes</th>
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<td>4</td>
<td>0.16</td>
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<tr>
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<td>0.16</td>
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Bibliography
Basic references


Complementary references


