

Multidimensional Distributions

Code: 104857
ECTS Credits: 6

2024/2025

Degree	Type	Year
2503852 Applied Statistics	OB	2

Contact

Name: Antoni Sintes Blanc
Email: antoni.sintes@uab.cat

Teaching groups languages

You can view this information at the [end](#) of this document.

Prerequisites

Elementary probability. Real random variables. Differential and integral calculation. Elemental algebra: vector spaces and determinants.

Objectives and Contextualisation

The probability distribution of a random vector (discrete or continuous) is the main objective of this course.

We analyze the principal characteristics of the joint distribution: the vector of means, the variance-covariance matrix, the

marginal and conditional distributions, etc.

As a principal example we study the multidimensional normal distribution. It is an important continuous distribution, with applications in linear

model theory, multivariate analysis and statistical decision theory.

Theory and calculations related to continuous multidimensional distributions, strongly depends on integral and differential calculus

with functions of several variables. Having this in mind, we review the principal technics focusing on multivariate probability

applications.

Learning Outcomes

1. KM10 (Knowledge) Describe the characteristics of the distribution and density functions of random variables.

Content

1. Random vectors.

k-dimensional random vectors. The component variables of a random vector. Definition of the joint law of a random vector:

the discrete case and the absolutely continuous case. The joint probability distribution function. Bivariate discrete finite

distributions: marginal and conditional distributions.

2. Discrete distributions.

General bivariate discrete distributions. Marginal distributions. Multivariate discrete distributions. Marginal distributions.

The multinomial distribution. Functions of a discrete random vector.

3. Continuous distributions.

General bivariate continuous distributions. Marginal distributions. Multivariate continuous distributions. Marginal

distributions. Functions of a continuous random vector.

4. Independence and conditional distributions.

Statistically independent random variables and joint distributions. Conditional distributions: discrete and continuous case.

5. Mathematical expectation and other numerical characteristics.

Expectation of a function of a random vector. The moment generation function. Covariance and correlation coefficient.

The variance-covariance matrix. Conditional expectation. Conditional variance. The double expectation theorem.

6. The multidimensional normal distribution.

The bidimensional normal distribution. The multidimensional normal distribution. Distributions related to the normal

distribution: chi-square distributions, Student t distributions and Fisher-Snedecor F distributions. Student theorem.

Cochran theorem.

Unless the requirements enforced by the health authorities demand a prioritization or reduction of these contents.

Activities and Methodology

Title	Hours	ECTS	Learning Outcomes
-------	-------	------	-------------------

Type: Directed

Theory lessons	28	1.12
Type: Supervised		
Computer laboratory practical sessions (with Maxima and R)	14	0.56
Practical lessons about problems and exercises	14	0.56
Type: Autonomous		
Personal work dossier (exercices and theory)	22	0.88

Teaching methodology is based on the following activities and material:

- Theory lessons.
- Practical lessons about problems and exercises.
- Computer laboratory practical sessions (with Maxima and R).
- Personal work dossier (DTP).
- Theory and problem textbooks.
- Study and personal work weekly guides (GETPS).
- Course workspace on the UAB Virtual Campus Moodle.

The proposed teaching methodology may experience some modifications depending on the restrictions to face-to-face activities enforced by health authorities.

Annotation: Within the schedule set by the centre or degree programme, 15 minutes of one class will be reserved for students to evaluate their lecturers and their courses or modules through questionnaires.

Assessment

Continous Assessment Activities

Title	Weighting	Hours	ECTS	Learning Outcomes
Classroom problems (EA)	10%	14	0.56	
Computer lab work (with Maxima and R)	0% to 10%	14	0.56	
Final examinations (EF1, EF2)	0% to 50%	0	0	KM10
Partial examinations (EP1, EP2)	20% to 40% (each one)	0	0	KM10
Personal work dossier of exercices and theory (DTP)	10% to 20%	44	1.76	

Continued evaluation:

Continued evaluation students can obtain up to 40% of the total score with personal work, done along the course:

personal work dossier (DTP), computer lab work (PRC) and classroom problems (EA), if delivered within the term.

The remaining score is covered by two (independent and equal weight) partial examinations, EP1 and EP2, both with a

second-chance examination, EF1 and EF2.

To pass the course, is required to obtain a minimum of 30% in each of both partial examinations, as well as a minimum of 50%

of the total score.

Denote DTP, EA, PRC, EP1, EP2, EF1 and EF2 the points (over 10) obtained on each of these evaluation items. Then the final

global punctuation QF (over 10) is calculated by means of the next formula:

$$QF = TC + 0.05 (10-TC-TC1) [\max(EP1, EF1) + \max(EP2, EF2)]$$

where $TC = 0.2 DTP + 0.1 EA + 0.1 PRC$ and $TC1 = \max(0, 1 - 0.2 DTP) + (1 - 0.1 EA)$.

The minimum condition on partial examinations is: $\min\{\max(EP1, EF1), \max(EP2, EF2)\} \geq 3$

If this condition is not satisfied then the final global punctuation is $\min(QF, 4.5)$.

Single evaluation:

Single evaluation students will have a final exam and a recovery.

The final exam will be held on a single day or on two consecutive days and will have two parts, with a maximum duration of 3 hours each.

The content of the first part of the exam will be the same as that of the EP1 exam (partial 1 of the continuous evaluation). We will denote AU1 the qualification of this exam, over 10.

The content of the second part of the exam will be the same as that of the EP2 exam (partial 2 of the continuous evaluation). We will denote AU2 the qualification of this exam, over 10.

If the condition $\min(AU1, AU2) \geq 3.5$ is met, the final grade is calculated as $QFU = (AU1 + AU2)/2$, and the course is passed if $QFU \geq 5$.

Otherwise, you have to take the recovery exam.

The recovery exam will be held on a single day or on two consecutive days and will have two parts, with a maximum duration of 3 hours each.

The content of the first part of the exam will be the same as that of the EP1 exam (part 1 of the continuous evaluation). We will denote AUR1 the qualification of this exam, out of 10.

The content of the second part of the exam will be the same as that of the EP2 exam (partial 2 of the continuous evaluation). We will denote AUR2 the qualification of this exam, out of 10.

The minimum condition in this case is: $\min\{\max(AU1, AUR1), \max(AU2, AUR2)\} \geq 3.5$, and the final grade is calculated as

$$QFUR = 0.7 ([\max(AU1, AUR1) + \max(AU2, AUR2)]/2) + 0.3 QFU$$

If the minimum condition is not met, the final overall score is $\min(QFUR, 4.5)$.

Student's assessment may experience some modifications depending on the restrictions

to face-to-face activities enforced by health authorities.

Bibliography

J.E. Marsden & J. Tromba: *Calculo Vectorial* (Addison-Wesley).

M. de Groot: *Probabilidad y Estadística* (Addison-Wesley).

D. Peña: *Fundamentos de Estadística* (Alianza Editorial).(*)

D. Peña: *Análisis de datos multivariantes* (McGraw-Hill).(*)

J.G. Kalbfleisch: *Probabilidad e Inferencia Estadística* (Vol. 1) (AC).

R.P. Dobrow: *Introduction to Stochastic Processes with R* (Wiley)

V. Zaiats; M.L. Calle; R. Presas: *Probabilitat i Estadística. Exercicis I*. U.A.B. (Materials, 107).(*)

(*) most relevant bibliography.

Software

- R Core Team (2021). R: A language and environment for statistical computing. R Foundation for Statistical Computing, Vienna, Austria. URL <https://www.R-project.org/>.
- wxMaxima (C) 2004-2018 Andrej Vodopivec

Language list

Name	Group	Language	Semester	Turn
(PAUL) Classroom practices	1	Catalan	first semester	afternoon
(PLAB) Practical laboratories	1	Catalan	first semester	afternoon
(PLAB) Practical laboratories	2	Catalan	first semester	afternoon
(TE) Theory	1	Catalan	first semester	afternoon